

# Metal Structures

## Design Project II

### Floor girders – examples of calculation (part II)

### III<sup>rd</sup> example of calculations – rigid joint

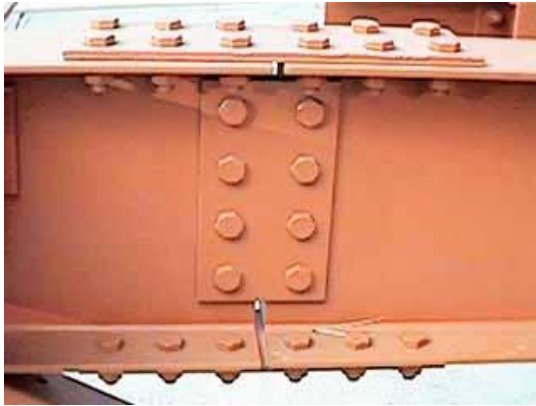


Photo: amsd.co.uk

Rigid joint, primary beam - primary beam, two transport members

New complex of data

HEA 650

Bending moment  $M_{Ed} = 727,8 \text{ kN m}$

Vertical force  $V_{Ed} = 162,2 \text{ kN}$

Axial force  $N_{Ed} = 0,0 \text{ kN}$

S235

$f_y = 235 \text{ MPa}$

Analysis of bolted joint concerns few important questions:

- Initial assumptions about geometry of joint → #t / 4 – 5
- Distribution of loads in joint → #t / 6 – 11
- Initial analysis of bolts (category of joint, class of bolt, dimension, length, geometry) → #t / 12 – 27
- Distribution of external actions between bolts → #t / 28 – 34
- Stiffness of joint (according assumption – rigid joint) → #t / 35
- Checking of resistances → #t / 36 – 79

## Initial assumptions about geometry

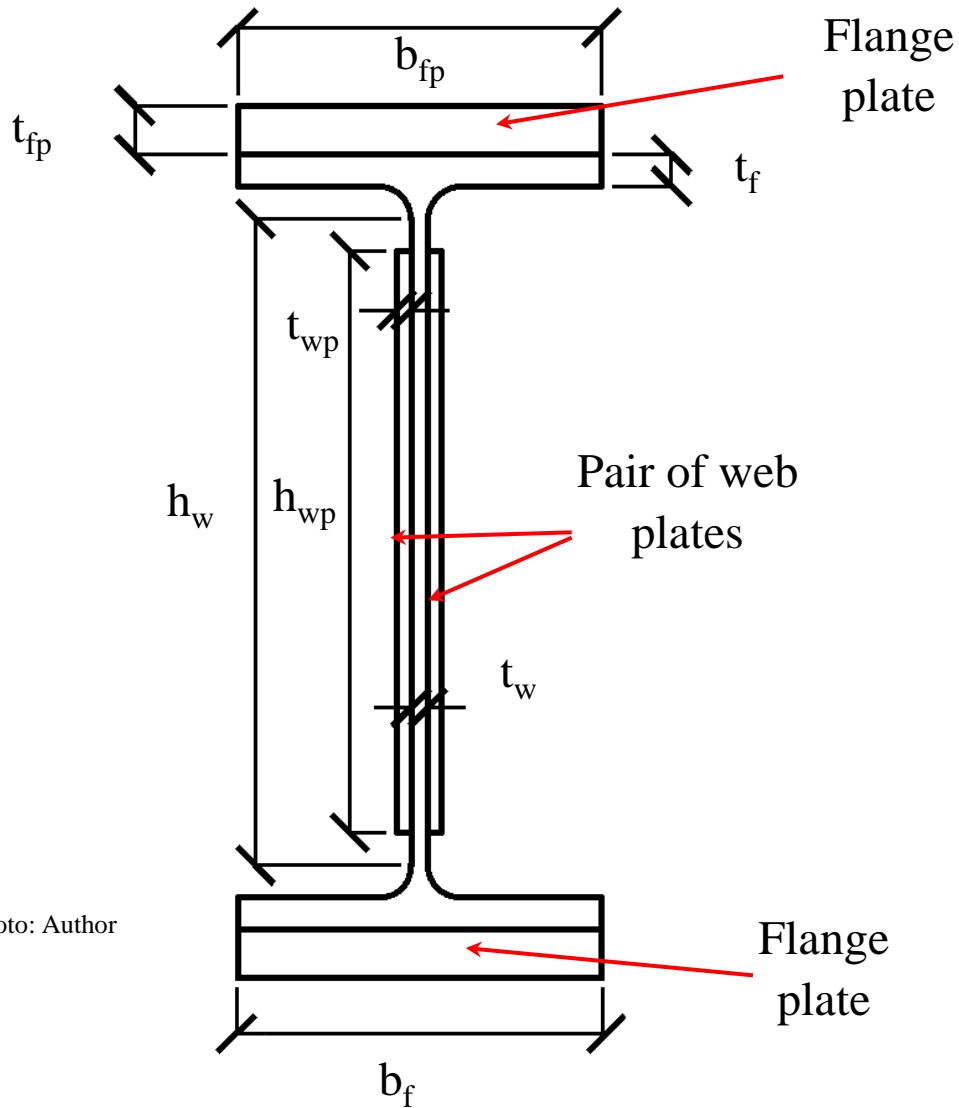


Photo: Author

## Recommendation:

$$b_{fp} = b_f$$

$$t_f \leq t_{fp} \leq 2t_f$$

$$t_{wp} \leq t_w \leq 2t_{wp}$$

$$t_{wp} \geq 8 \text{ mm}$$

$$h_{wp} \approx 0,8 h_w$$

## Initial checking of geometry:

$$0,8 J_{I, y} \leq J_{fp, y}$$

$$J_{fp, y} \geq 10 J_{wp, y}$$

HEA 650, geometry

I<sup>st</sup> class of cross-section

$$J_y = 175\,200 \text{ cm}^4$$

$$h = 640 \text{ mm}$$

$$t_w = 13,5 \text{ mm}$$

$$h_w = 534 \text{ mm}$$

$$t_f = 26 \text{ mm}$$

$$b_f = 300 \text{ mm}$$

$$r = 27 \text{ mm}$$

You must remember: **plates of some thickness are not produced or not recommended:**

...20, 21, 22, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46... [mm]

$$b_{fp} = b_f = 300 \text{ mm}$$

$$t_f \leq t_{fp} \leq 2t_f \rightarrow 26 \leq t_{fp} \leq 52 \rightarrow t_{fp} = 30 \text{ mm}$$

$$t_{wp} \leq t_w \leq 2t_{wp} \rightarrow t_{wp} \leq 13,5 \leq 2t_{wp}$$

$$t_{wp} \geq 8 \text{ mm}$$

$$t_{wp} = 12 \text{ mm}$$

$$h_{wp} \approx 0,8 h_w \rightarrow h_{wp} \approx 427 \text{ mm} \rightarrow h_{wp} = 420 \text{ mm}$$

$$0,8 J_{I, y} = 140\,160 \text{ cm}^4 \leq J_{fp, y} = 202\,000 \text{ cm}^4 \quad \text{OK}$$

$$J_{fp, y} = 202\,000 \text{ cm}^4 \geq 10 J_{wp, y} = 148\,176 \text{ cm}^4 \quad \text{OK}$$

# Shear joint, distribution of cross-sectional forces

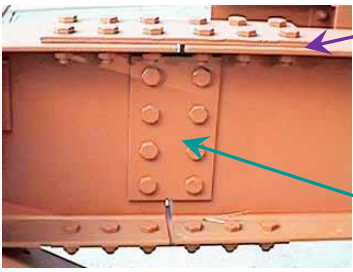


Photo: amsd.co.uk

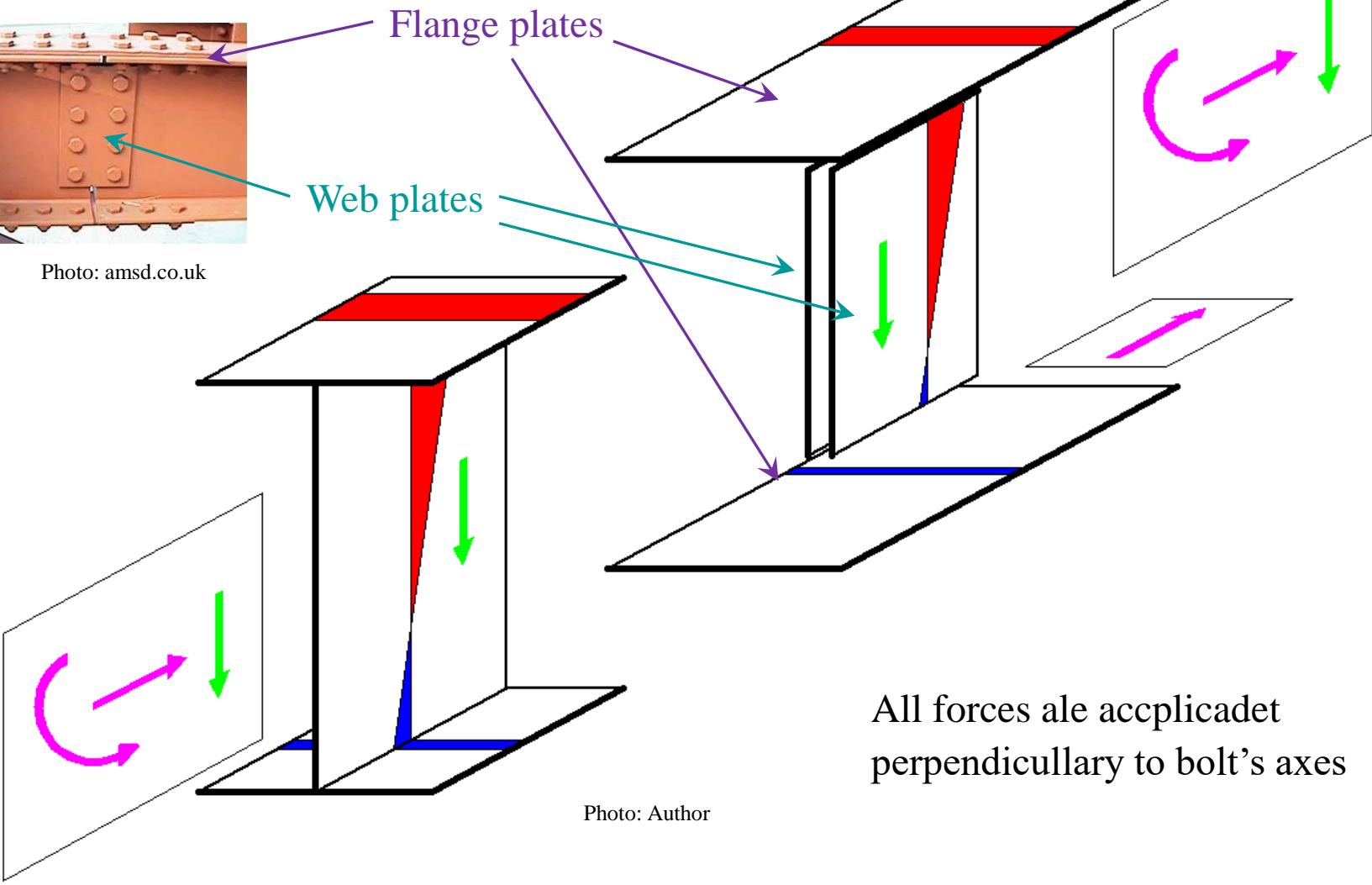


Photo: Author

All forces are applied perpendicular to bolt's axes

Recommendation: in proportion to geometrical characteristics of flange (f) and web (w):

$$M_{fp} = M_{Ed} J_{f,y} / J_{I,y}$$

$$M_{wp} = M_{Ed} J_{w,y} / J_{I,y}$$

$$N_{fp} = N_{Ed} A_f / A_I$$

$$N_{wp} = N_{Ed} A_w / A_I$$

$$V_{fp} = 0$$

$$V_{wp} = V_{Ed}$$

$$J_{f,y} \approx (\text{Steiner's theorem only}) \approx \\ \approx 2 b_f t_f (h / 2 - t_f / 2)^2 = 147\,028 \text{ cm}^4$$

$$J_{w,y} \approx J_{I,y} - J_{f,y} = 28\,172 \text{ cm}^4$$

$$M_{fp} = 610,770 \text{ kNm}$$

$$M_{wp} = 117,030 \text{ kNm}$$

No external axial force:

$$N_{fp} = 0,0 \text{ kN}$$

$$N_{wp} = 0,0 \text{ kN}$$

$$V_{fp} = 0$$

$$V_{wp} = 162,200 \text{ kN}$$

These cross-sectional force act on both parts of joint in the same value

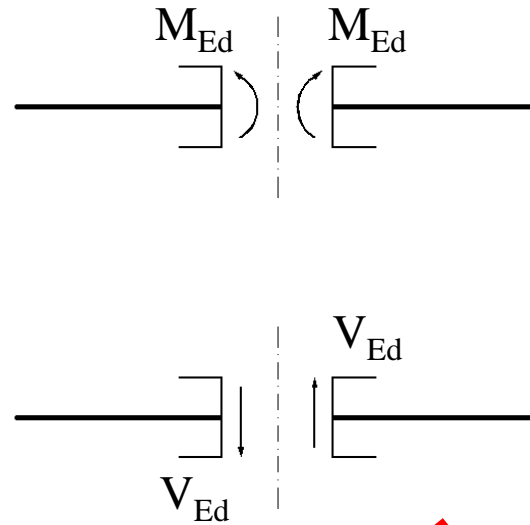
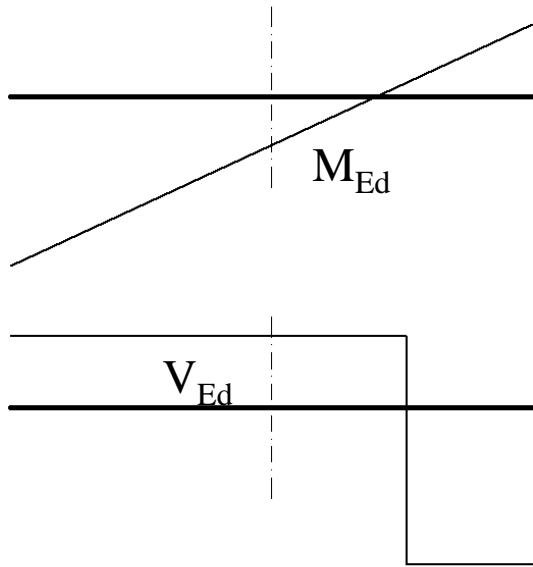
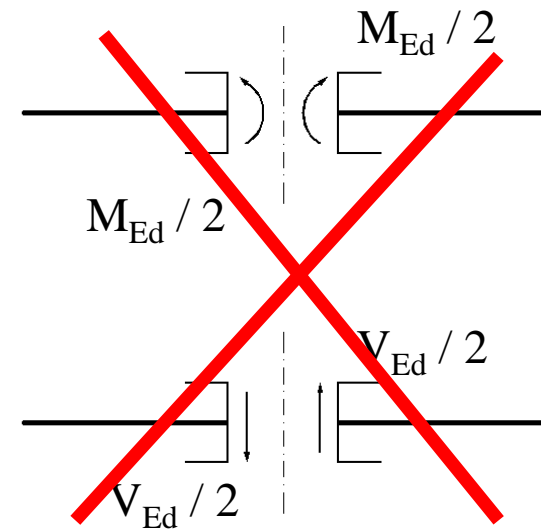


Photo: Author

Common mistake: half of values on both parts on joint



## Recalculation from global forces to local forces in plates

Flange plate, in general case: part of global axial force ( $N_{fp}$ ; in analysed case = 0) +/- one of couple of forces from bending moment applied to flange plate ( $M_{fp}$ );

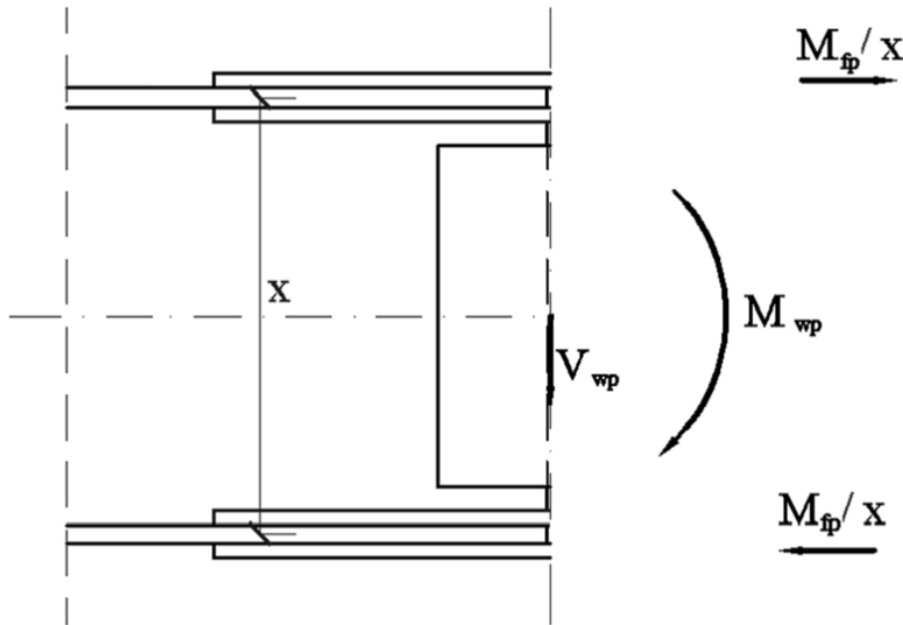


Photo: Author

$$x = h - t_f / 2 - t_f / 2 = 588 \text{ mm}$$

$$F_{fp} = | M_{fp} | / x = 1037,724 \text{ kN}$$

Web plate: part of axian force ( $N_{wp}$ ; in analysed case = 0); part of bending moment ( $M_{wp}$ );  
total external shear force ( $V_{wp} = V_{Ed}$ )

## Initial checking resistance

Flange plate:

$$F_{fp} / [ 0,8 (0,5 A_{fp}) f_y ] \leq 1,0$$

Web plate:

$$\sigma = N_{wp} / (0,8 A_{wp}) + M_{wp} / (0,8 W_{wp,y})$$

$$\tau = V_{wp} / A_{wp}$$

$$[\sqrt{(\sigma^2 + 3\tau^2)}] / f_y \leq 1,0$$

**0,5**  $A_{fp} \rightarrow A_{fp}$  it is area of **both** flange plates (the same:  $J_{f,y}$  means moment of inertia **both** flanges); here is analysed only **one** flange plate (more stressed);

**0,8**  $\rightarrow$  initial assumption about netto geometry of plates (cross-section without holes for bolts); phenomenon not important for shear force.

$$A_{fp} = 180,0 \text{ cm}^2$$

$$F_{fp} / [ 0,8 (0,5 A_{fp}) f_y ] = 0,613 \leq 1,0 \quad \text{OK}$$

$$\sigma = M_{wp} / (0,8 W_{wp,y})$$

$$\tau = V_{wp} / A_{wp}$$

$$W_{wp,y} = 705,6 \text{ cm}^3$$

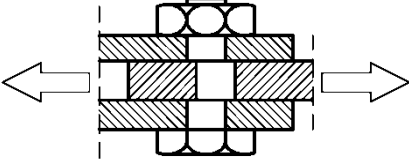
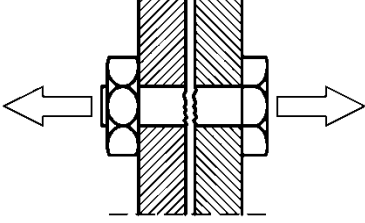
$$A_{wp} = 100,8 \text{ cm}^2$$

$$\sigma = 207,323 \text{ MPa}$$

$$\tau = 16,091 \text{ MPa}$$

$$[\sqrt{(\sigma^2 + 3\tau^2)}] / f_y = 0,890 \leq 1,0 \quad \text{OK}$$

### Categories of bolted joints and loads

					
Categories of bolted joint	A	B	C	D	E
Types of loads	Static without changing the direction of the bending moments; aerodynamic	Static with changing the direction of the bending moments; aerodynamic	Dynamic	Static; aerodynamic	Dynamic
Types of bolts	„normal”	preloaded		„normal”	preloaded

Changing the direction of the bending moment:  
various combinations of loads

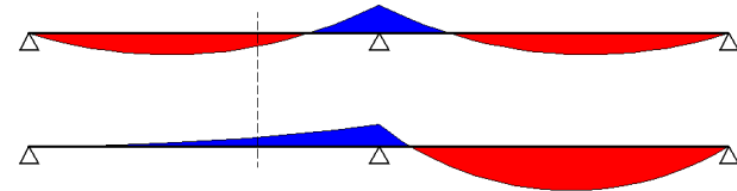


Photo: Author

Loads are static only. Various combinations of actions: checking direction of bending moment.

It will be bolted joint category B.

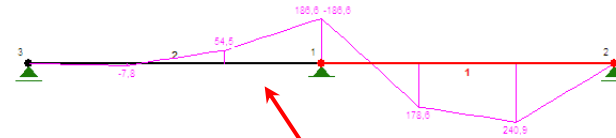
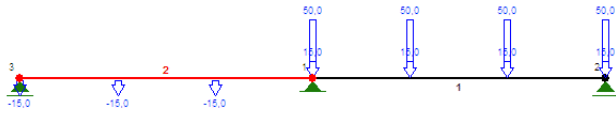
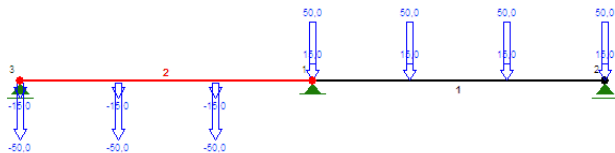


Photo: Author

Checking direction of bending moment in joint



According to results of experiments, we can assume, that there are always pinned joints, if:

→ #14 / 42

- web only is supported;
- for bolts are applied slotted holes.

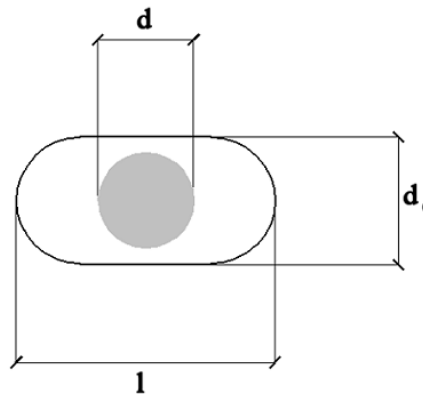
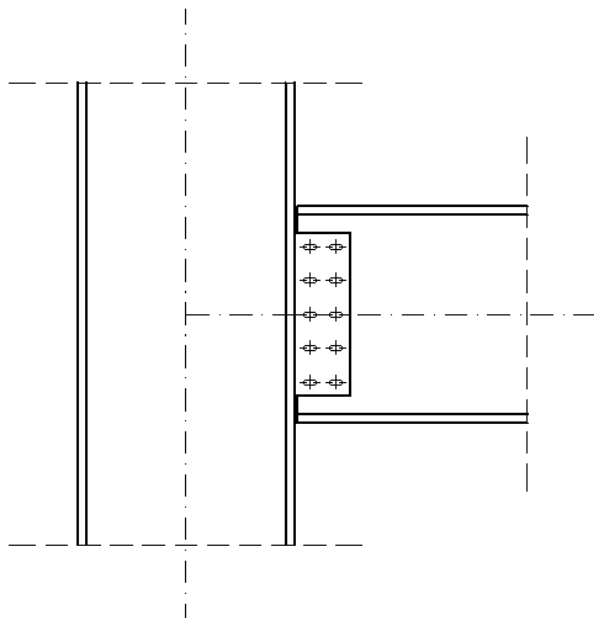


Photo: Author



Photo: tekla-detailed-structural-fabrication.com

Of course, slotted holes can be used for compensation of imperfection during erection of structures. The technical solutions used at that time are heading towards the development of a rigid joint.

But other solutions allow to get an pinned joint with them.

→ #14 / 43

Photo: Author

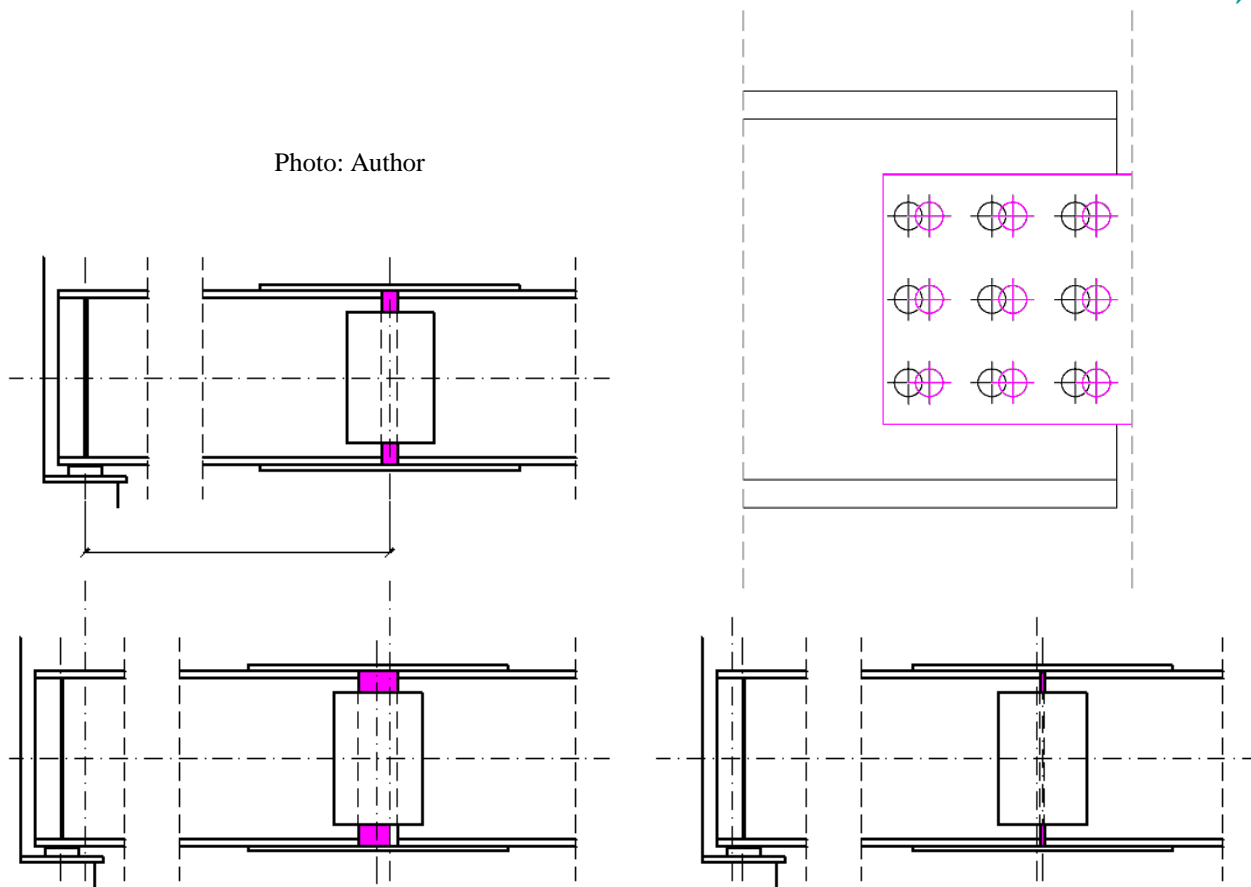


Photo: tekla-detailed-structural-fabrication.com

Previous part of calculation (Des #2 Ex #1):  
slotted holes applied to ensure **hinge joint**

At now:

slotted holes in **rigid joint** to avoid problems with imperfections.

Generally: slotted holes can make hinge joint (in bolteg joint **category A**), but after application additional specific technical solution (preloaded bolts, bolted joint **category B or C**), joint will can be taken into consideration as rigid.

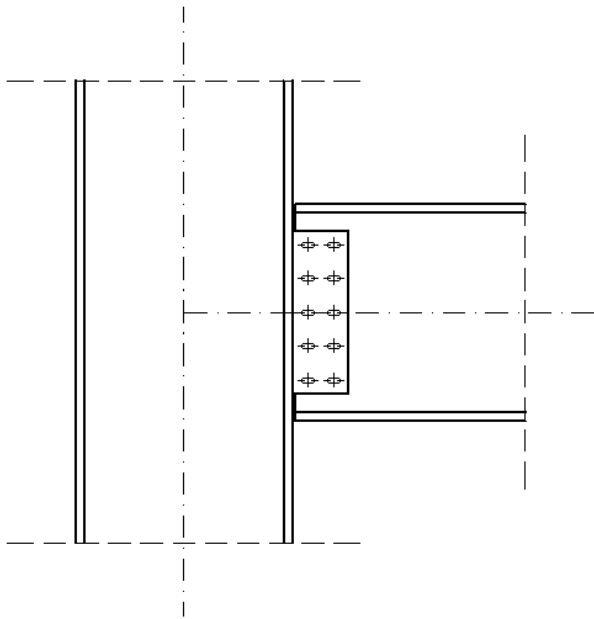
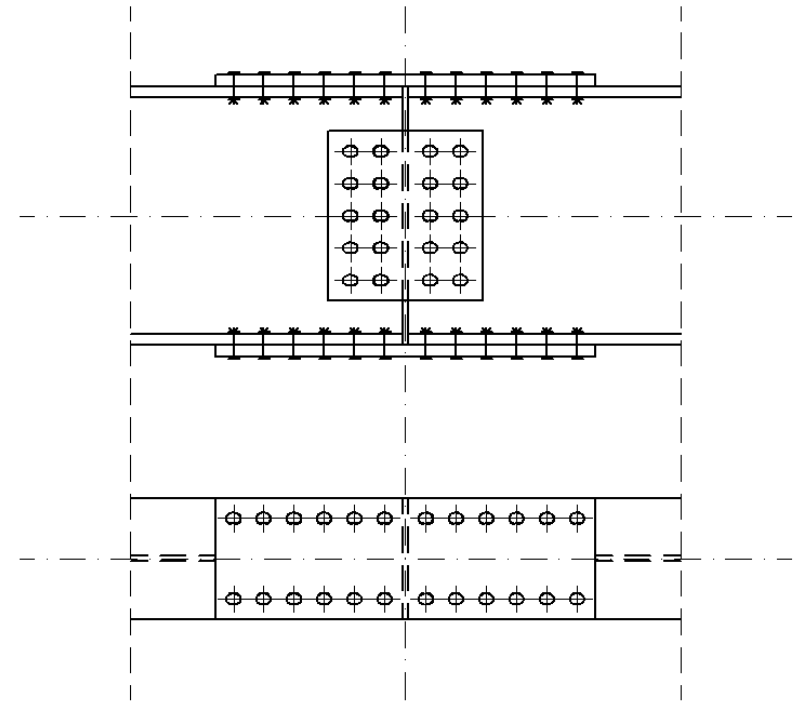


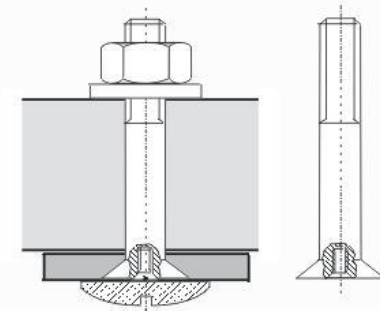
Photo: Author



Differences between two diameters:  $d_0 - d =$  or  $l - d =$  [mm]

Bolts or pins:		M 12, M 14	M16, M 18, M 20, M 22	M 24	M 27, M 30 ...
Fit bolts		0			
Normal <u>round</u> holes		1 (0,5) 2	2 (1,5)		3 (2,5)
Oversize <u>round</u> holes		3	4	6	8
Short <u>slotted</u> holes	$d_0$	1 2	2		3
	1	4	6	8	10
Long <u>slotted</u> holes	$d_0$	1 2	2		3
	1	1,5 d			

EN 1090-2 tab 11  
(mast, towers)  
countersunk bolts



Rivets - nominal hole diameter shall be specified individually in each design project

Photo: zeglarstwo.sail-ho.pl

Bolts:

Symbol:

M16 → d = 16mm

Category	Class	Diameter
A, D	4.6, 4.8	d = 16 mm
	5.6, 5.8, 6.8	d = 20 - 24 mm
	8.8, 10.9	d ≥ 24 mm
B	8.8, 10.9	d ≥ 24 mm
C, E		

Class: X.Y

$$X = f_{ub} / 100 \rightarrow f_{ub} = 100 X$$

$$Y = 10 f_{yb} / f_{ub} \rightarrow f_{yb} = 10 X Y$$

Class: 4.8

$$f_{ub} = 400 \text{ MPa}$$

$$f_{yb} = 320 \text{ MPa}$$

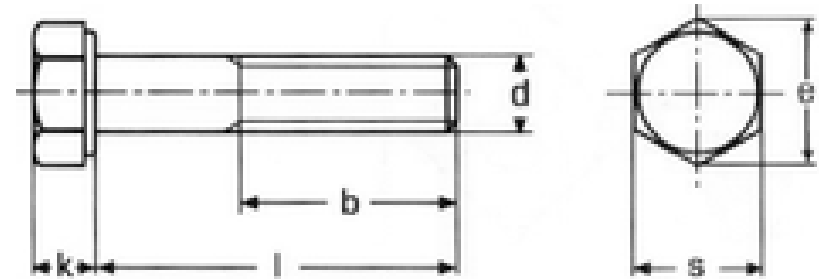


Photo: Author

**Bolted joint category B** means, that classes 8.8 and 10.9 are recommended. There will be taken into consideration **class 8.8**.

$$f_{ub} = 800 \text{ MPa}$$

$$f_{yb} = 640 \text{ MPa}$$

For this class, diameter of bolt non smaller than 24 mm is recommended. There will be taken into consideration **bolt M24**

$$d = 24 \text{ mm}$$

$$A = 4,52 \text{ cm}^2 \quad (\text{unthreaded portion cross-section})$$

$$A_s = 3,53 \text{ cm}^2 \quad (\text{threaded portion cross-section})$$

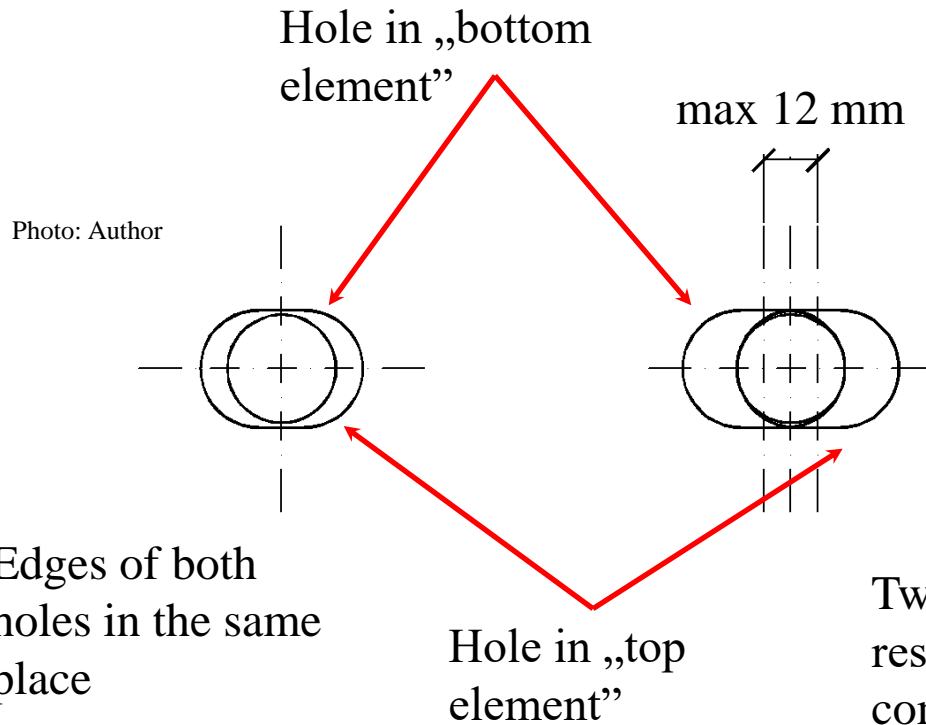
**Long slotted holes** (for avoiding of imperfections) will be applied:

$$d_0 = d + 2 \text{ mm} = 26 \text{ mm}$$

$$l = 1,5 d = 36 \text{ mm}$$

Ideal situation:

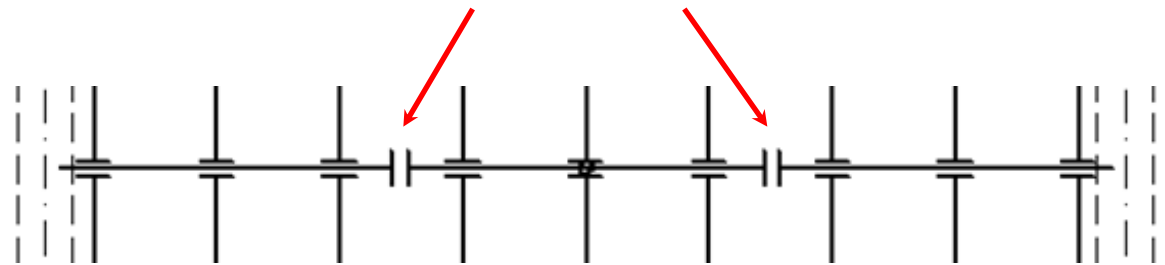
Real situation (impact of imperfections):



Max distance between edges of holes in „top” and „bottom element” (plate and flange / web of beam)

Two joints for construction site, on each 12 mm reserve for imperfections → possibility of compensation of 24 mm imperfection (non-intentional shifts on supports).

Photo: Author



Verification of initial assumptions about bolt: M24, class 8.8 (recommendations):

$$1,5 t_{\min} \leq d \leq 2,5 t_{\min}$$

Category A, D:  $\Sigma t \leq 5d$

Category B, C, E:  $\Sigma t \leq 8d$

$$f_{ub} > f_u$$

Min. thickness of each  
elements connected by bolt

Web - web plate:  $t_{\min} = 12 \text{ mm}$

Flange - flange plate:  $t_{\min} = 26 \text{ mm}$

$$1,5 t_{\min} = 18 \text{ mm} \leq d = 24 \leq 2,5 t_{\min} = 30 \text{ mm}$$

$$1,5 t_{\min} = 39 \text{ mm} \leq d = 24 \leq 2,5 t_{\min} = 65 \text{ mm}$$

not satisfied

OK

$$\Sigma t = 12 + 13,5 + 12 = 38 \text{ mm} \leq 8d = 192 \text{ mm}$$

OK

This is recommendation only, not Eurocore  
requirement. It is possible that it will not be  
satisfied.

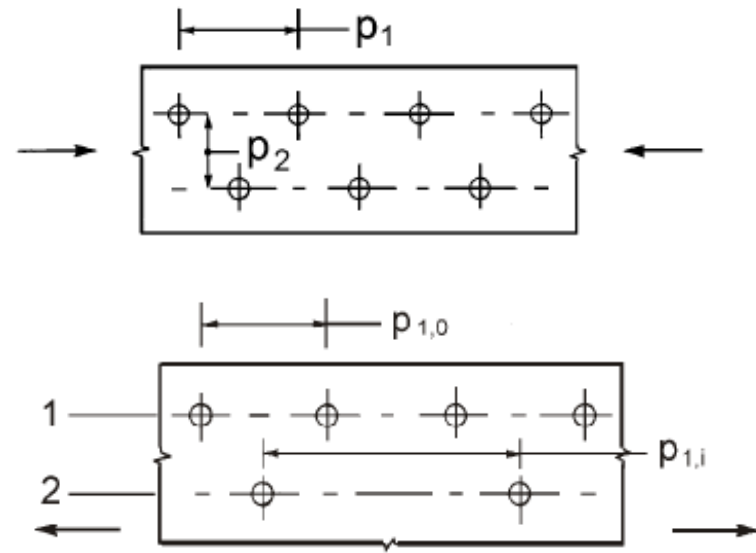
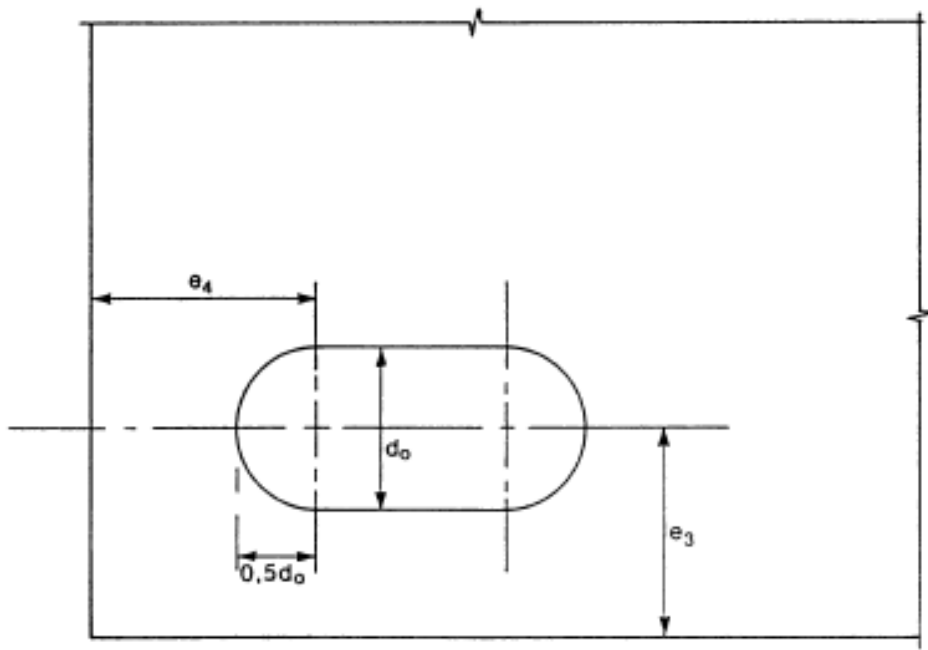
$$\Sigma t = 26 + 30 = 56 \text{ mm} \leq 8d = 192 \text{ mm}$$

OK

$$f_{ub} = 800 \text{ MPa} > f_u = 360 \text{ MPa} \quad \text{OK}$$



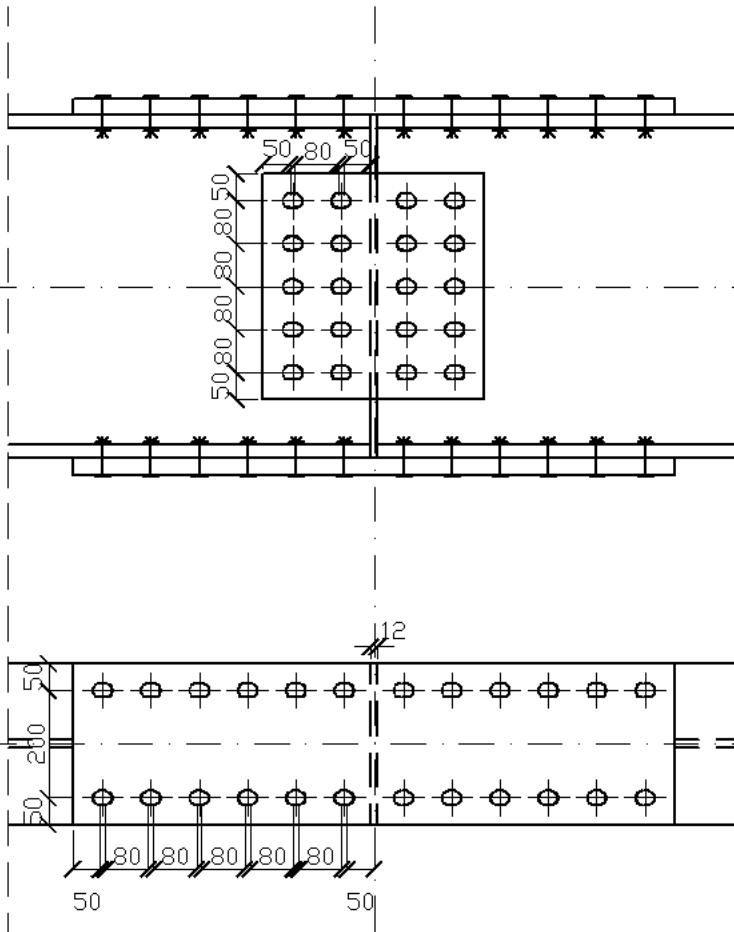
Distances according to EN 1993-1-8 fig. 3.1



Dimensions	Minimum	Maximum		
		„Normal” steels		Stainless steels
		Steel exposed to the weather / corrosion influences	Not exposed	
$e_1$	$1,2 d_0$	$4 t_{e, \min} + 40 \text{ mm}$		$\max(8 t_{e, \min} ; 125 \text{ mm})$
$e_2$	$1,2 d_0$	$4 t_{e, \min} + 40 \text{ mm}$		$\max(8 t_{e, \min} ; 125 \text{ mm})$
$e_3$	$1,5 d_0$			
$e_4$	$1,5 d_0$			
$p_1$	$2,2 d_0$	$\min(14 t_{e, \min} ; 200 \text{ mm})$	$\min(14 t_{e, \min} ; 200 \text{ mm})$	$\min(14 t_{\min} ; 175 \text{ mm})$
$p_{1,0}$		$\min(14 t_{e, \min} ; 200 \text{ mm})$		
$p_{1,i}$		$\min(14 t_{e, \min} ; 200 \text{ mm})$		
$p_2$	$2,4 d_0$ ( $1,2 d_0$ and $L \geq 2,4 d_0$ )	$\min(14 t_{e, \min} ; 200 \text{ mm})$	$\min(14 t_{e, \min} ; 200 \text{ mm})$	$\min(14 t_{\min} ; 175 \text{ mm})$

Flange:

One direction of external force  
only



Dim.	min [mm]	max [mm]	real [mm]	Concl.
$e_1 (e_4)$	36	144	50	OK
$e_2 (e_3)$	36	144	50	OK
$p_1$	56	200	80	OK
$p_2$	62	200	200	OK

In case of compressive axial force:

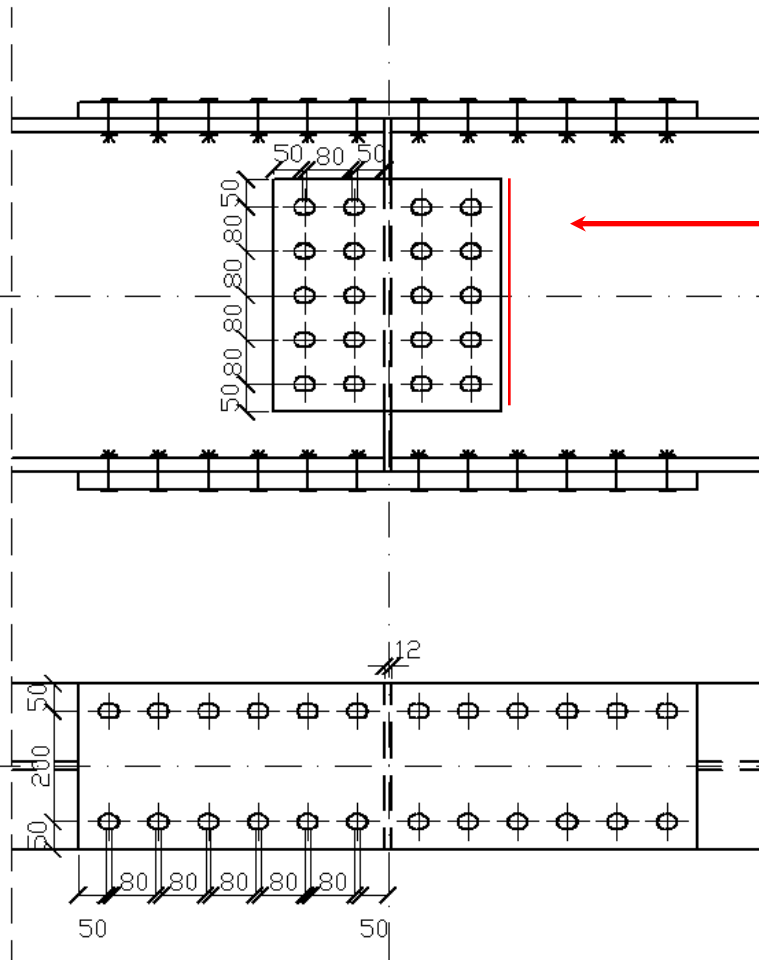
$$p_1 / t < 9\varepsilon$$

$$\varepsilon (S235) = 1,0 \quad ; \quad t = 30 \text{ mm}$$

$$80 / 30 = 2,667 < 9 \text{ OK}$$

Photo: Author





Common mistake in student projects:  
initially assumed height of web plate

$$h_{wp} \approx 0,8 h_w$$

is different from the final adopted height

$$2 \cdot e + n \cdot p$$

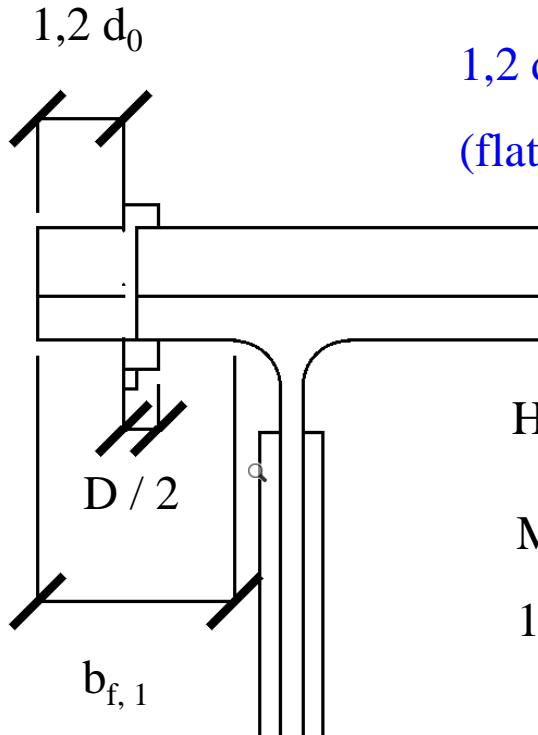
**It must be one and the same value:**

$$h_{wp} \approx 0,8 h_w \approx 420 \text{ mm}$$

$$50 + 4 \cdot 80 + 50 = 420 \text{ mm}$$

Photo: Author

Additional limit: enough space on flange



$$1,2 d_0 + D / 2 + 5 \text{ mm} \leq b_{f,1}$$

(flat part of flange)

$$\text{HEA 650: } b_{f,1} = (300 - 2 \cdot 27 - 13,5) / 2 = 116 \text{ mm}$$

$$\text{M24: } 1,2 d_0 = 31,2 \text{ mm} \quad ; \quad D / 2 = 20,8 \text{ mm}$$

$$1,2 d_0 + D / 2 + 5 \text{ mm} = 57 \text{ mm} \leq b_{f,1} \quad \text{OK}$$

Otherwise, we risk that nut will get stuck on rounded part between web and flange and we will not be able to tighten bolt.

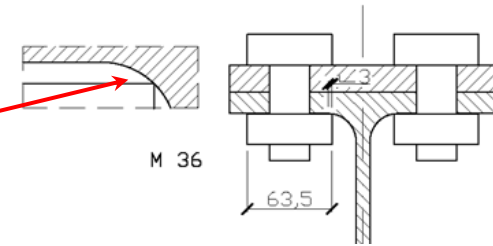
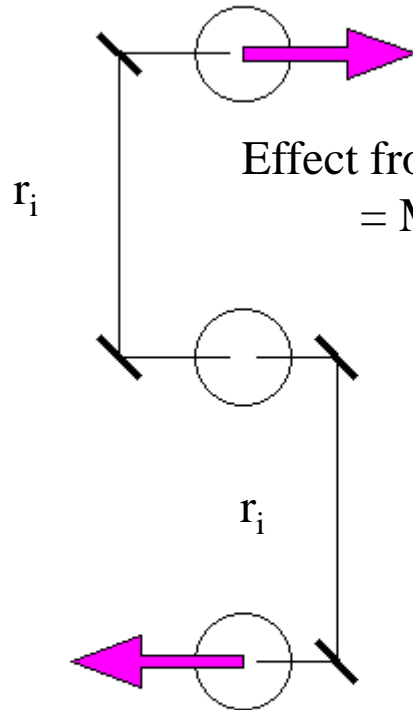
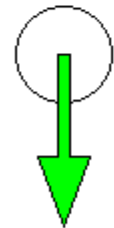
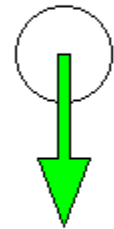
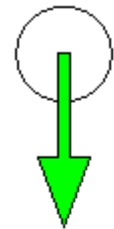


Photo: Author

## Distribution of forces:

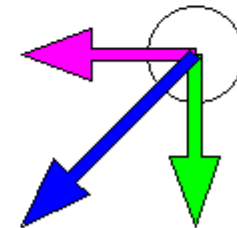
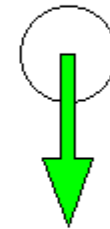
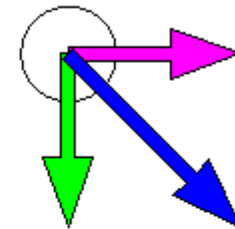
Photo: Author

Effect from bending moment:  
always perpendicular to arm  $r$   
between **center of bolts group** and  
analysed bolt.



$$\text{Effect from bending moment} = M_{Ed} \cdot r_i / \sum [(r_i)^2]$$

$$\sum [(r_i)^2] \neq [\sum (r_i)]^2$$



Resultants

Vertical force per one bolt =  
= total force / number of bolts

→ Des #2 examp 1 / 55

## Distribution of forces, flange

Force in bolt = Force in flange / number of bolts on one side of joint

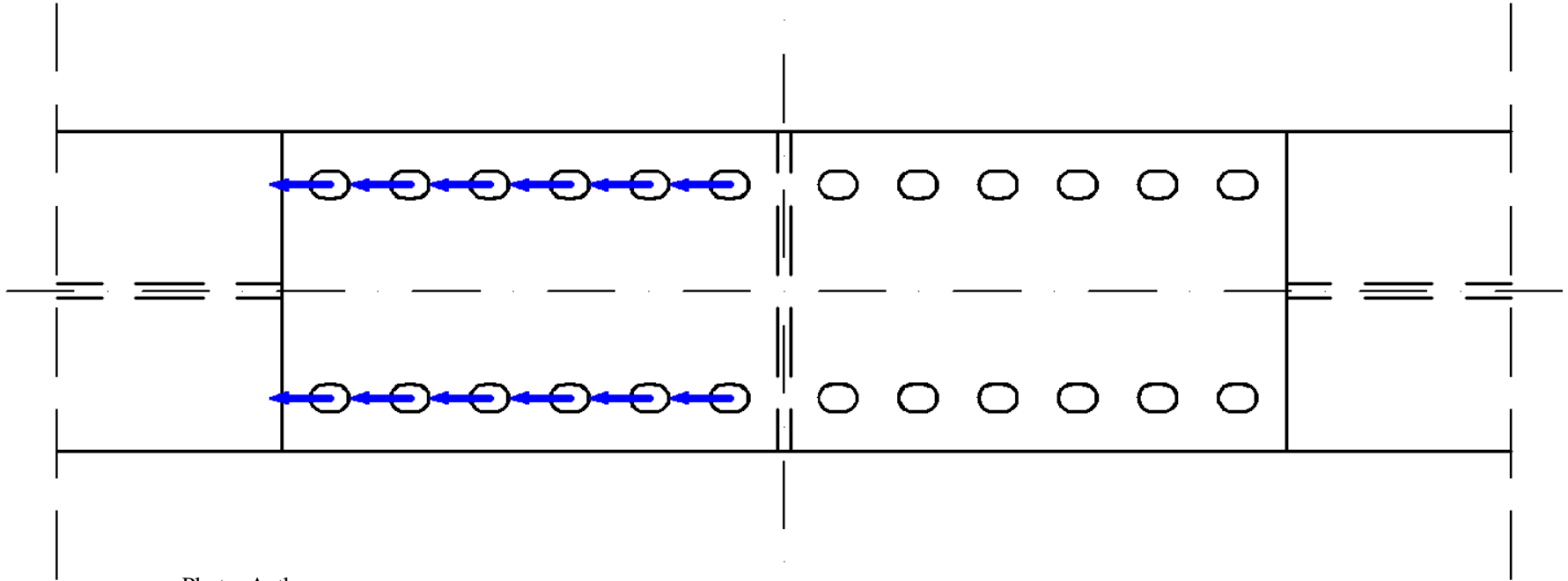


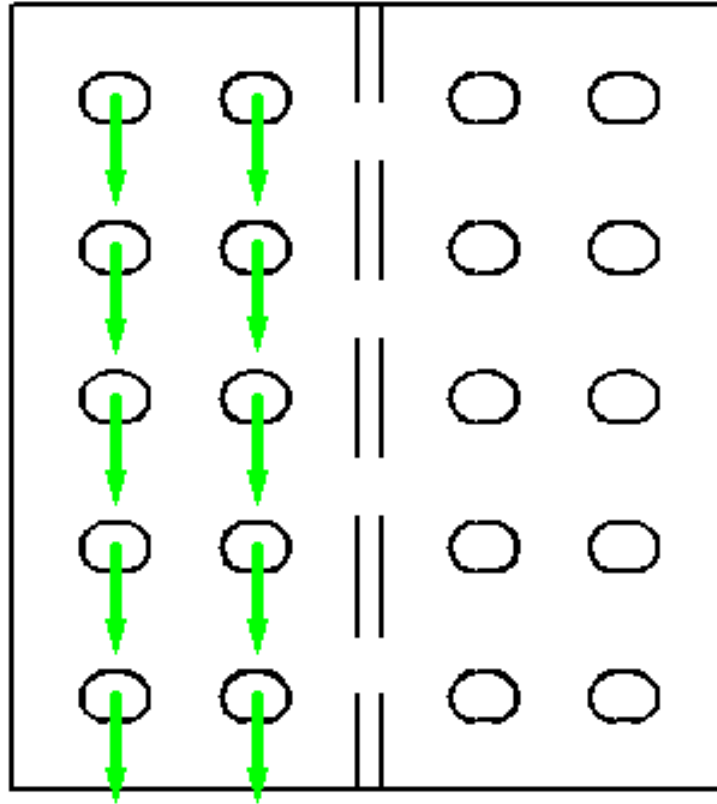
Photo: Author

$$F_{bf} = 1037,724 \text{ kN} / 12 = 86,477 \text{ kN}$$

## Distribution of forces, web

First force in bolt = Shear force in web / number of bolts on one side of joint

Photo: Author



$$F_{bf} = 162,200 \text{ kN} / 10 = 16,220 \text{ kN}$$

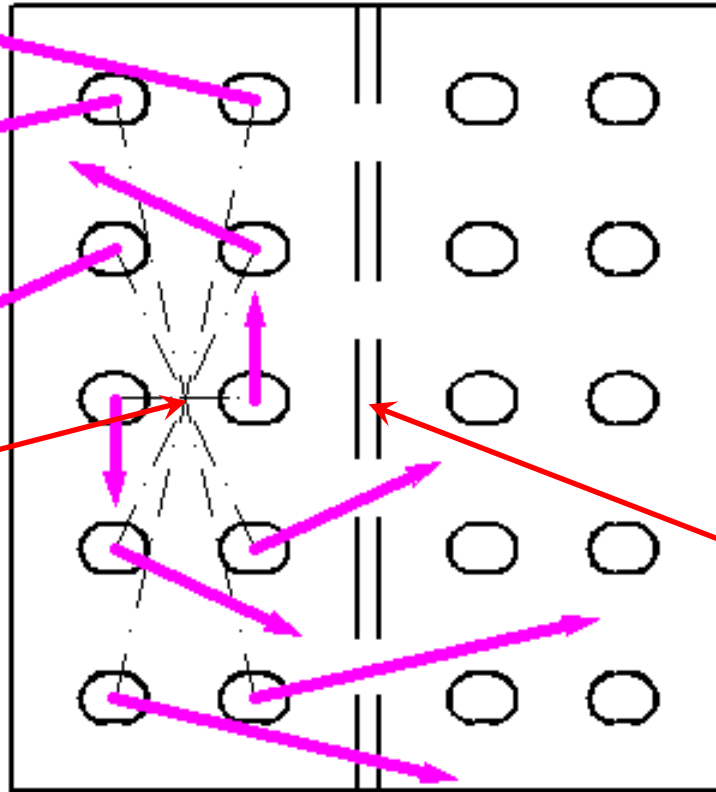
# Distribution of forces, web

$$\text{Second force in bolt} = M_{Ed} \cdot r_i / \Sigma [(r_i)^2]$$

$$\Sigma [(r_i)^2] \neq [\Sigma (r_i)]^2$$

Photo: Author

Centre of gravity for group of bolts on one side of joint



Common mistake in student projects:

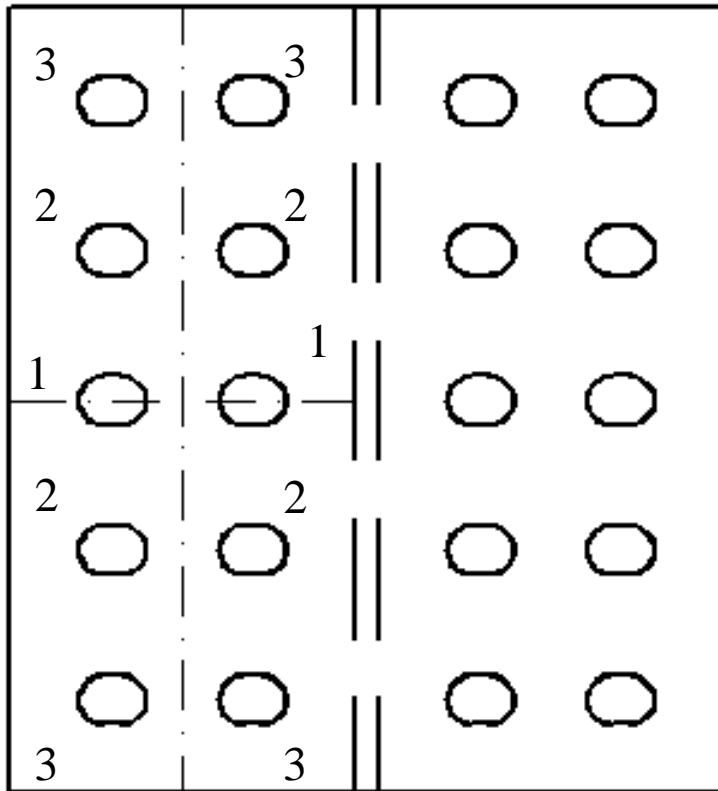
Centre of gravity of total joint, not group of bolts, is taken into consideration

Effect of bending moment is in proportion to length of arm and perpendicular to arm

# Distribution of forces, web

Because of horizontal and vertical axes of symmetry, only three bolts will be analysed

Photo: Author

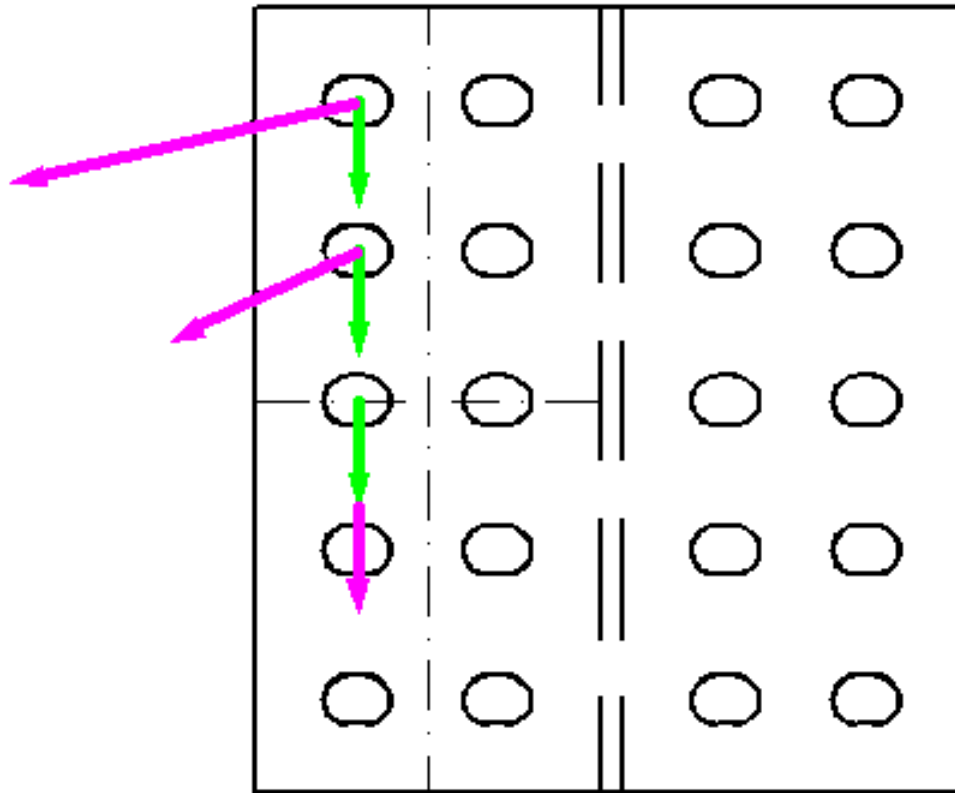


$$r_1 = 37,5 \text{ mm} = 0,0375 \text{ m}$$

$$r_2 = 88,4 \text{ mm} = 0,0884 \text{ m}$$

$$r_3 = 164,3 \text{ mm} = 0,1643 \text{ m}$$

$$\Sigma [(r_i)^2] = 2 (r_1)^2 + 4 (r_2)^2 + 4 (r_3)^2 = 0,142 \text{ m}^2$$



Common effect from shear force and bending moment (example for three bolts).

For each bolt: sum of these forces will be converted into two components, horizontal and vertical.

## Distribution of forces, web

Bolt	Part from shear force (vertical) [kN]	Vertical part from bending moment [kN]	Horizontal part from bending moment [kN]	$\Sigma V$ [kN]	$\Sigma H$ [kN]	Product [kN]
1	16,220	30,906	0,000	47,126	0,000	47,126
2	16,220	30,906	65,975	47,126	65,975	81,077
3	16,220	30,906	131,835	47,126	131,835	140,005

## Stiffness of joint

According to #15 / 69-70, shear bolted joint with bolts category B or C, can be treated as rigid joint. This means, that real behaviour of joint is the same as in initial assumption (rigid joint). Each formulas from Eurocode can be applied without any changes, that would result from behavior of semi-rigid joint.

# Resistance of bolted joint category B: six mechanisms of destruction:

Shear resistance



Photo: ceptros.civil.tamu.edu

Bearing resistance  
(local deformation of plate)



Photo: ascelibrary.org

Block tearing (total destruction of plate)



Photo: quora.com

Netto area (other type of total destruction of plate)



Photo: quora.com

Slip-resistant (too small friction between elements)

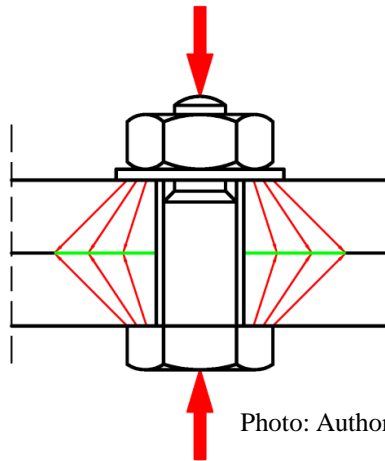


Photo: Author

Punching resistance (local destruction of plate)

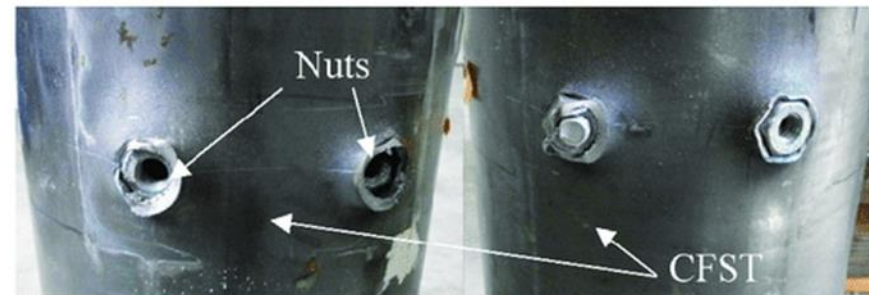


Photo: Moment Resisting Connection with Curved Endplates: Behaviour Study, A. Mudrow & all

Loads:

## Shear resistance



Photo: ceprocs.civil.tamu.edu

Total force applied to one bolt:

Flange bolt: 86,477 kN

Web bolt :

First bolt: 47,126 kN

Second bolt: 81,077 kN

Third bolt: 140,005 kN

## Bearing resistance



Photo: ascelibrary.org

Two perpendicular force, separately in the first and second directions:

Flange plate (one direction of load only): 86,477 kN

Web plate:

Around first bolt: 47,126 kN ; 0,000 kN

Around second bolt: 47,126 kN ; 65,975 kN

Around third bolt: 47,124 kN ; 131,835 kN

Loads:

Slip-resistant:

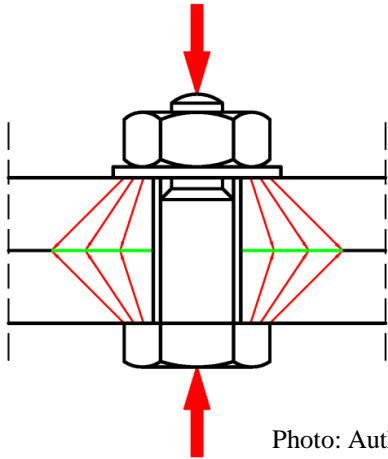


Photo: Author

Total force applicated to one bolt,  
but for category B **in characteristic values:**

Flange bolt: 57,985 kN

Web bolt :

First bolt: 32,234 kN

Second bolt: 55,457 kN

Third bolt: 95,763 kN

**Characteristic values** → #t / 39

Punching resistance

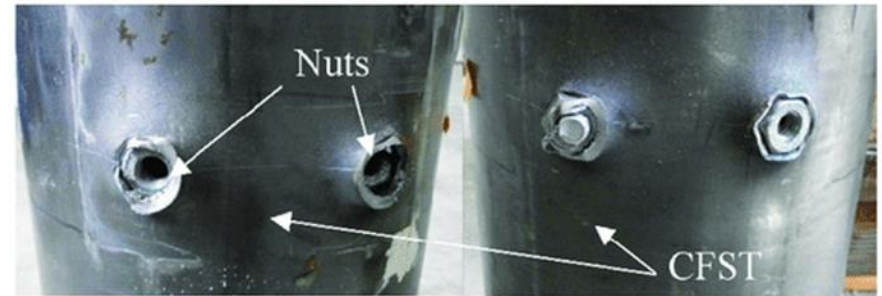


Photo: Moment Resisting Connection with Curved Endplates:  
Behaviour Study, A. Mudrow & all

Value of preloading force needed to obtain friction  
(results from resistance in case of slip-resist)

For category B in characteristic values:

Cross-sectional forces comes from loads:

$$g_k = 3,53 \text{ kN} / \text{m}^2$$

$$g_d = 1,35 \cdot 3,53 = 4,776 \text{ kN} / \text{m}^2$$

$$q_k = 10,00 \text{ kN} / \text{m}^2$$

$$q_d = 1,5 \cdot 10,00 = 15,00 \text{ kN} / \text{m}^2$$

$$g_k + q_k = 13,53$$

$$g_d + q_d = 19,776$$

$$k / d = 13,53 / 19,776 = 0,684$$

Cross-sectional forces in characteristic values could be taken as 68,4% of its design values.

## Loads:

### Netto area



Photo: quora.com

Similar phenomena. The only difference is shape of break line and type of load (straight or almost-straight line and many loads for netto area; straight or broken line and one force for block tearing)

### Block tearing



Photo: quora.com

In both cases total loads, applicated to member

Member	Netto area	Block tearing (phenomenon calculated for one direction of force only)
Flange plate	1037,724 kN	
Web plate	117,030 kNm and 162,200 kN	Many various loads, not taking into consideration
I-beam	727,800 kNm and 162,200 kN	

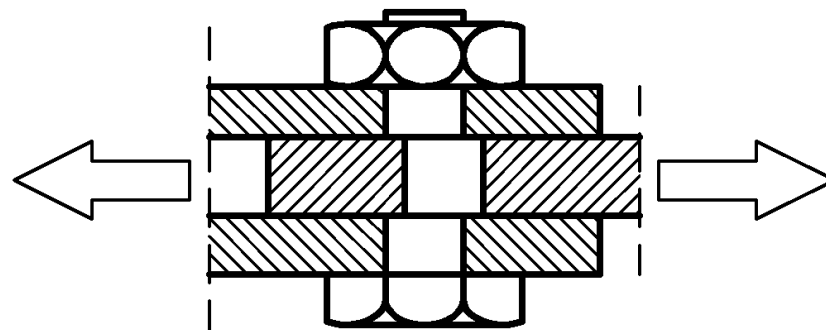
Shear resistance: destruction of shank of bolt

$$F_{V,Rd} = n \alpha_v f_{ub} A_b / \gamma_{M2} \quad \text{EN 1993-1-8 tab 3.4}$$

$$\gamma_{M2} = 1,25$$

→ Des #2 examp 1 / 66

Photo: Author



$A_b$  - area of unthreaded portion of bolt  $A$ , or threaded portion of bolt  $A_s$

$n$  - number of shear planes (in analysed case  $n = 1$ , between web of IPE 300 and vertical stiffener)

$\alpha_v$  :

$A_b = A_s$				$A_b = A$			
4.6	5.6	8.8		4.8	5.8	6.8	10.9
0,6			0,5				0,6

EN 1993-1-8 tab. 3.4

Recommendation type of bolt for category B: type HV with a thread along part of shank length according to EN 14 399-4

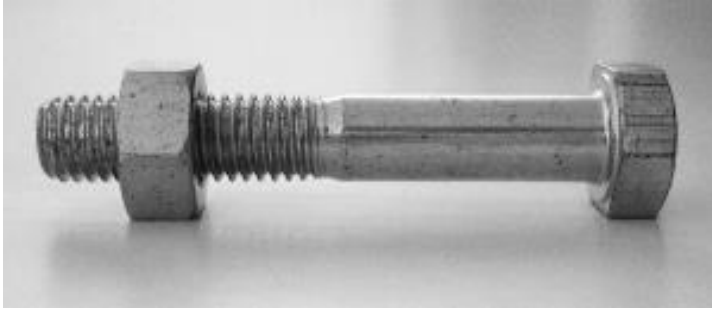


Photo: wikipedia



Photo: fxaball.co.uk

Categories B: two washers, under cup and nut

# Flange-flange plate: two possible bolt positions, "up" and "down".

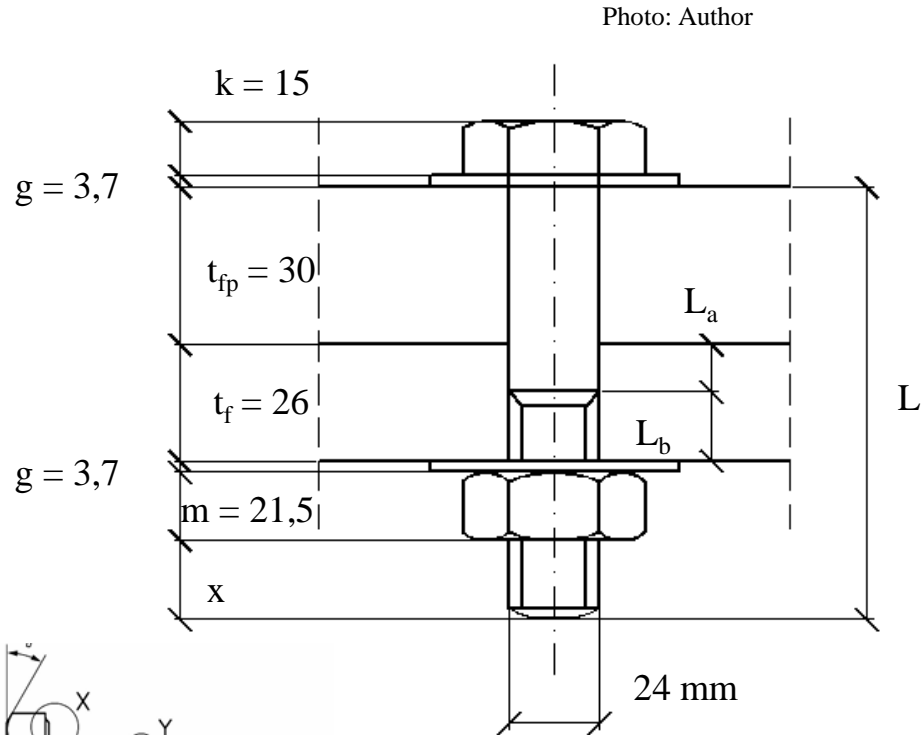
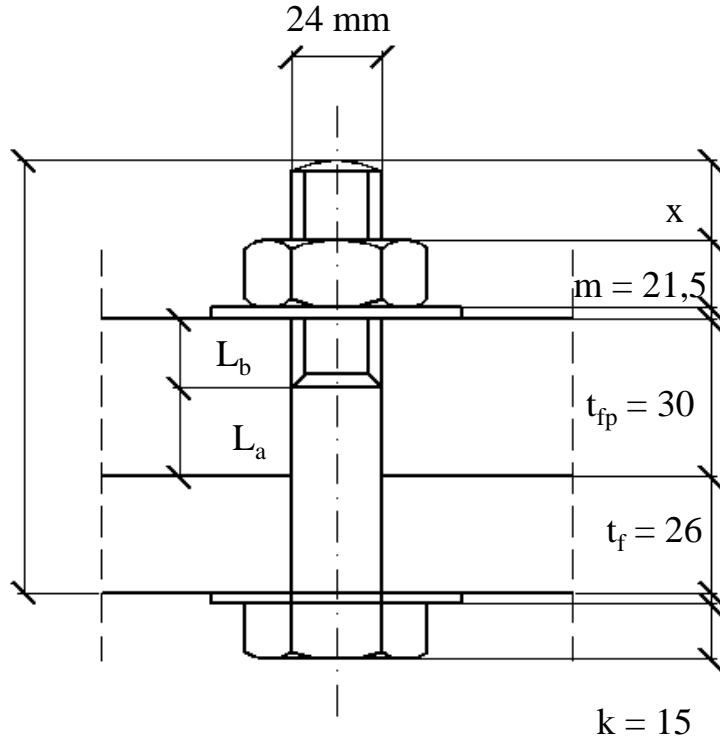


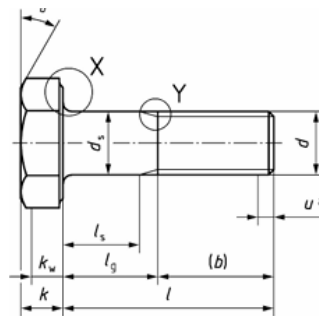
Photo: Author

$$4P = 12 \text{ mm} \leq x \leq d = 24 \text{ mm}$$

$$L_a \geq 2/3 \max(t_{fp} ; t_f) = 20 \text{ mm}$$

$$L_b \geq 4P = 12 \text{ mm}$$

$$L = x + m + g + t_f + t_{fp} + g = 97 - 109$$



$$l_s \geq \max(t_f + 2/3 t_{fp} ; 2/3 t_f + t_{fp}) = 48 \text{ mm}$$

Photo: EN 14 399-4 fig. 1

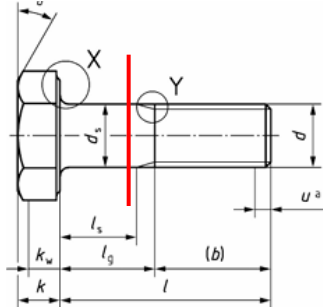


Photo: EN 14 399-4 fig. 1

Photo: EN 14 399-4 tab. 1

Thread (d)			M12		M16		M20		M22		M24		M27		M30		M36	
l			$l_s$ and $l_g^c$															
			$l_s$	$l_g$	$l_s$	$l_g$	$l_s$	$l_g$	$l_s$	$l_g$	$l_s$	$l_g$	$l_s$	$l_g$	$l_s$	$l_g$	$l_s$	$l_g$
nom.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.
35	33,75	36,25	6,75	12														
85	83,25	86,75	56,75	62	51	57	44,5	52	43,5	51	37	46	35	44	30,5	41	21	33
90	88,25	91,75	61,75	67	56	62	49,5	57	48,5	56	42	51	40	49	35,5	46	26	38
95	93,25	96,75	66,75	72	61	67	54,5	62	53,5	61	47	56	45	54	40,5	51	31	43
100	98,25	101,75			66	72	59,5	67	58,5	66	52	61	50	59	45,5	56	36	48
105	103,25	106,75			71	77	64,5	72	63,5	71	57	66	55	64	50,5	61	41	53

Shear plane goes through unthreaded part of bolt.  $A = 4,52 \text{ cm}^2$

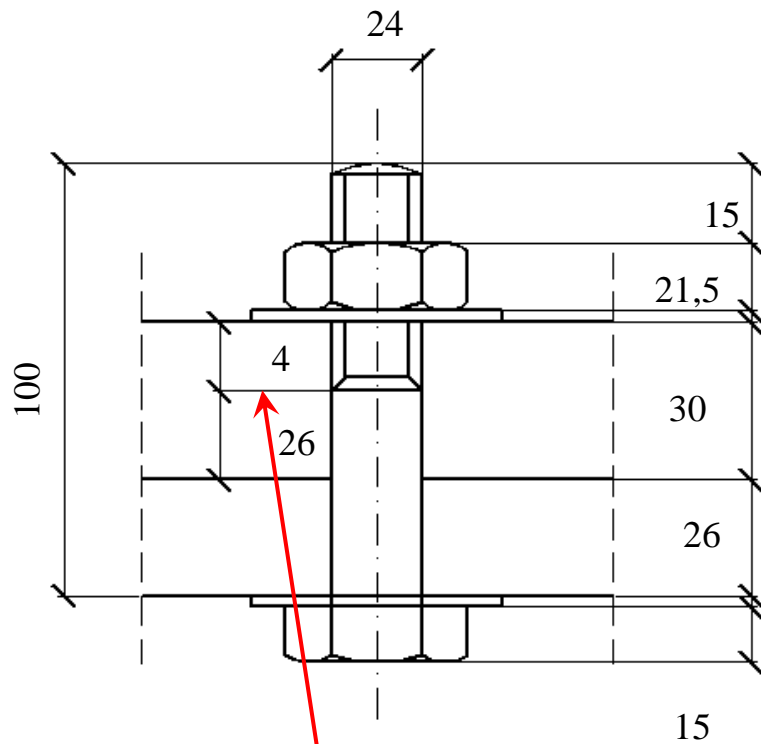
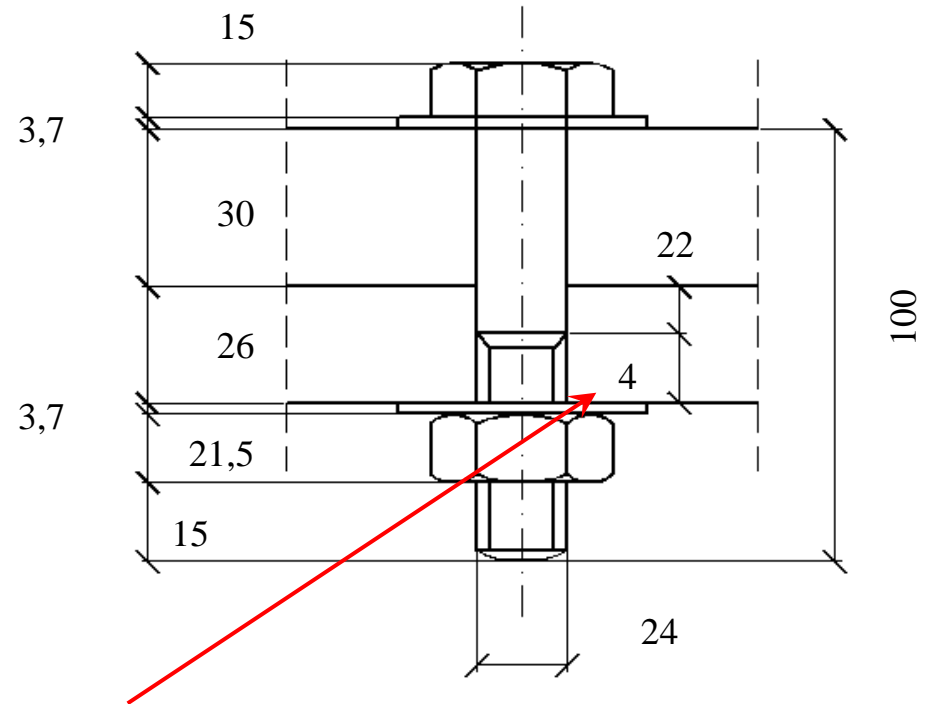


Photo: Author

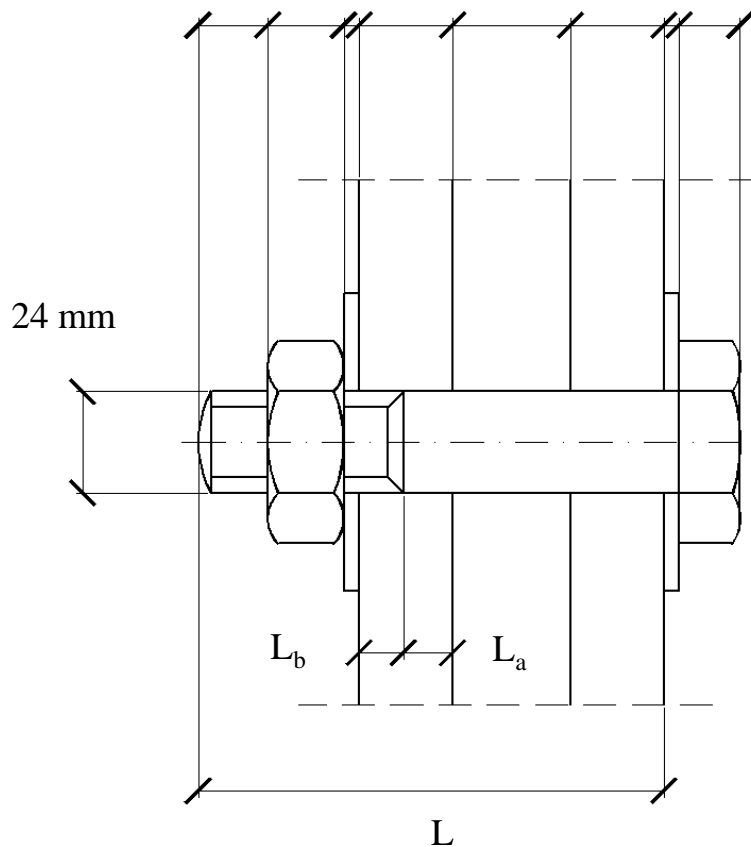


Does not meet recommendation  $> 4P = 12$  mm, but the rest is correct; accepted.

# Web - web plate: one possible bolt positions

$$m = 21,5 \quad t_{wp} = 12 \quad t_w = 12$$

$$x \quad g = 3,7 \quad t_w = 13,5 \quad g = 3,7$$



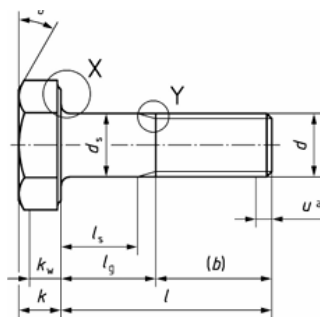
$$k = 15$$

$$4P = 12 \text{ mm} \leq x \leq d = 24 \text{ mm}$$

$$L_a \geq 2/3 t_{wp} = 8 \text{ mm}$$

$$L_b \geq 4P = 12 \text{ mm}$$

$$L = x + m + g + t_{wp} + t_w + t_{wp} + g = 78 - 90$$



$$l_s \geq 2/3 t_{wp} + t_w + t_{wp} = 34$$

Photo: Author

Photo: EN 14 399-4 fig. 1

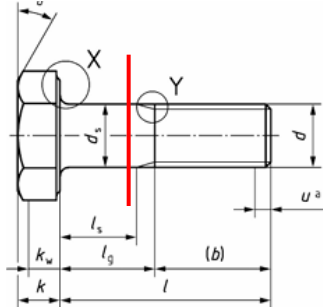


Photo: EN 14 399-4 fig. 1

Photo: EN 14 399-4 tab. 1

Thread (d)			M12		M16		M20		M22		M24		M27		M30		M36	
l			$l_s$ and $l_g$															
			$l_s$		$l_g$		$l_s$		$l_g$		$l_s$		$l_g$		$l_s$		$l_g$	
nom.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.	max.
75	73,5	76,5	46,75	52	41	47	34,5	42	33,5	41	27	36	25	34	20,5	31		
80	78,5	81,5	51,75	57	46	52	39,5	47	38,5	46	32	41	30	39	25,5	36		
85	83,25	86,75	56,75	62	51	57	44,5	52	43,5	51	37	46	35	44	30,5	41	21	33
90	88,25	91,75	61,75	67	56	62	49,5	57	48,5	56	42	51	40	49	35,5	46	26	38

Shear plane goes through unthreaded part of bolt.  $A = 4,52 \text{ cm}^2$

Web - web plate: one possible bolt positions

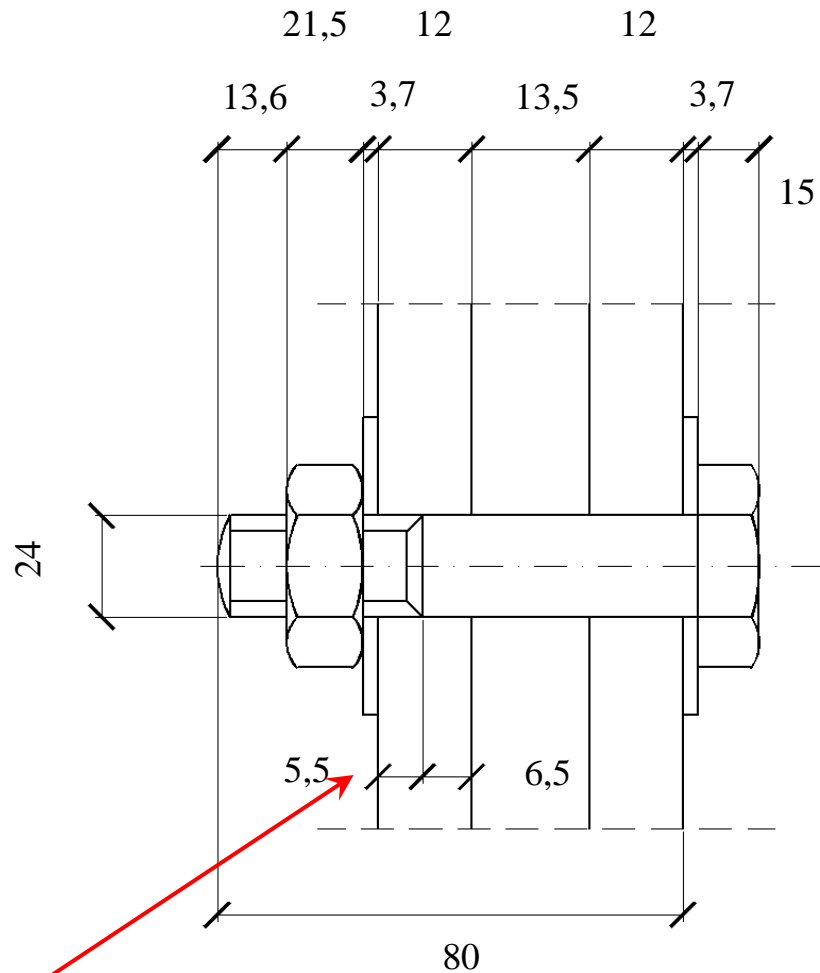


Photo: Author

Does not meet recommendation  $> 4P = 12$  mm, but the rest is correct; accepted.

d/l	M 12	M 16	M 20	M 22	M 24	M 27	M 30	M 36
30	48							
35	52							
40	56	105						
45	59	113	180					
50	64	121	194	249				
55	68	129	207	264				
60	72	137	219	279	353			
65	77	145	232	294	371			
70	81	153	244	309	389	519		
75	86	157	257	324	407	542	695	
80	90	165	269	339	425	564	723	
85	95	173	282	354	443	587	751	1186
90	99	181	288	363	449	609	779	1226
95	104	189	301	378	467	632	807	1266
100		197	313	393	485	645	832	1303
105		205	326	408	503	666	860	1343
110		213	338	423	521	687	888	1383
115		221	351	438	539	708	916	1423

Photo: euro-met.pl

Web – web plate unit mass 425 kg /  
1000 pcs

Flange – flange plate unit mass 485  
kg / 1000 pcs

**Flange** (n = 1, between flange plate and flange):

$$F_{V,Rd} = n \alpha_v f_{ub} A_b / \gamma_{M2} = 1 \cdot 0,6 \cdot 800 \text{ MPa} \cdot 4,52 \text{ cm}^2 / 1,25 = 173,568 \text{ kN}$$

**Web** (n = 2, between „left” web plate and web + between web and „right” web plate):

$$F_{V,Rd} = n \alpha_v f_{ub} A_b / \gamma_{M2} = 2 \cdot 0,6 \cdot 800 \text{ MPa} \cdot 4,52 \text{ cm}^2 / 1,25 = 347,136 \text{ kN}$$

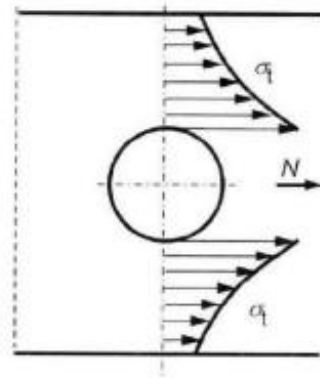
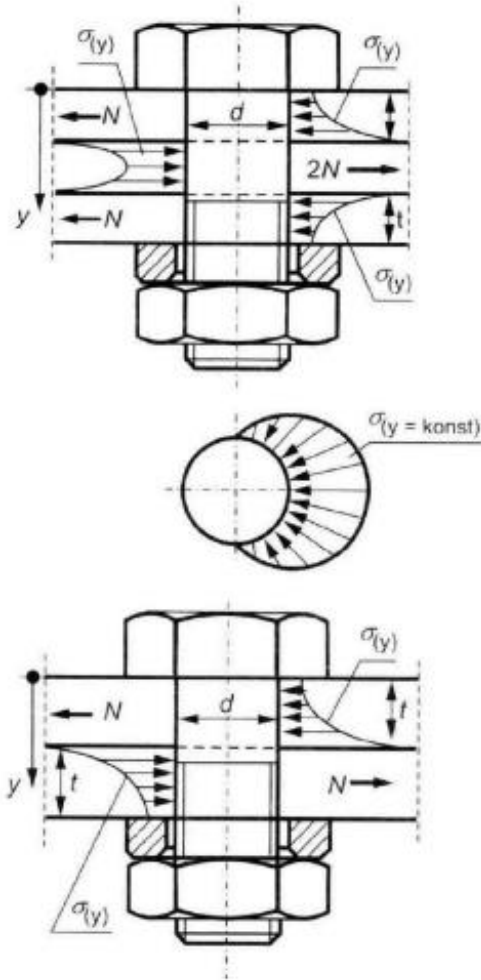
**Flange:**

$$86,477 / 173,568 = 0,498 < 1,0 \quad \text{OK}$$

**Web** (the most effort):

$$140,005 / 347,136 = 0,403 < 1,0 \quad \text{OK}$$

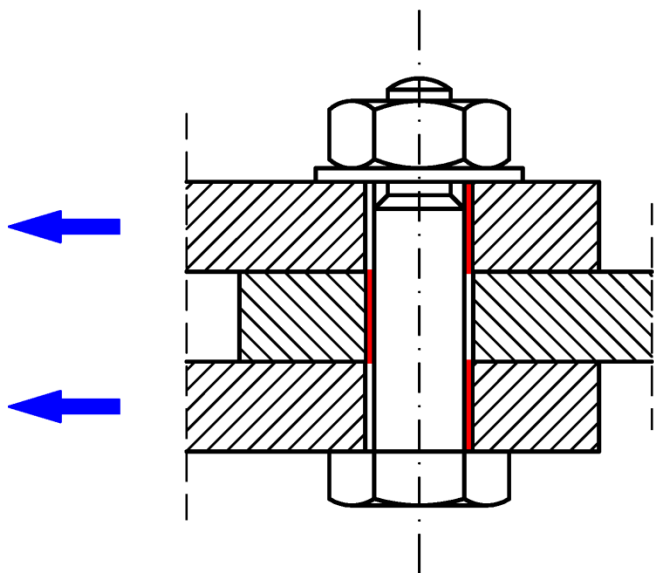
## Bearing resistance



Deformation or destruction of plates as the effect of contact with shank of bolt.

Photo: A. Biegus, Projektowanie konstrukcji stalowych według Eurokodów, Politechnika Wroclawska

→ Des #2 examp 1 / 68



→ Des #2 examp 1 / 70

$$F_{b,Rd} = \beta_b k_1 \alpha_b f_u d t_{\min} / \gamma_{M2}$$

Photo: Author

EN 1993-1-8 tab 3.4, **red part** is given in bottom part of table.

$\beta_b$  – parameter of shape of hole → Des#2Ex#1 / 71

$k_1$  – parameter for phenomenons in direction perpendicular  $\perp$  to force → Des#2Ex#1 / 72

$\alpha_b$  – parameter for phenomenons in direction parallel  $\parallel$  to force → Des#2Ex#1 / 71, 72

$f_u$  – ultimate strength of plate

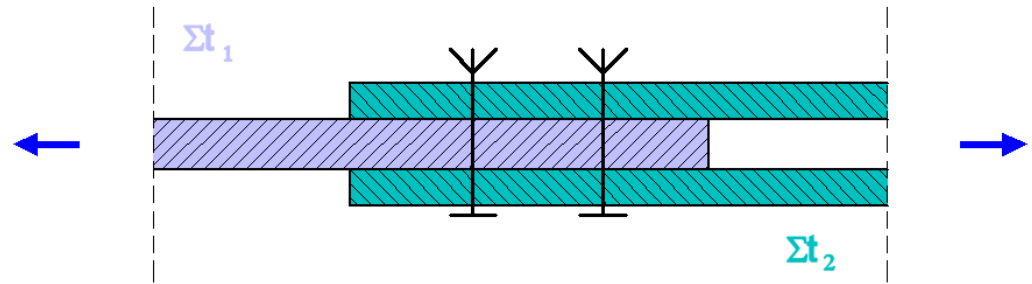
$d$  – dimension of bolt

$t_{\min}$  – minimum total thickness of plate → Des#2Ex#1 / 71

$$\gamma_{M2} = 1,25$$

$$\alpha_b = \min (\alpha_d ; f_{ub} / f_u ; 1,0)$$

$$t_{min} = \min (\Sigma t_1 ; \Sigma t_2)$$



→ Des #2 examp 1 / 71

Photo: Author

Intentionally: no resistance, allowing free movement along hole's axis. This allows beam to rotate, as in an ideal hinge. **After bolt has moved**, it may possibly come into contact with plate. Then coefficient can be assumed as for oversized round hole (to avoid damage of plate).

	$\beta_b$	
Fit bolts	1,0	
Normal round holes		
Oversized round holes	0,8	
Slotted holes	0,6	

EN 1993-1-8 tab 3.4

$k_1$  – parameter for phenomenons in direction perpendicular to force  $\perp$

$\alpha_b$  – parameter for phenomenons in direction parallel to force  $\parallel$

$$\alpha_b = \min (\alpha_d ; f_{ub} / f_u ; 1,0)$$

→ Des #2 examp 1 / 72

EN 1993-1-8 tab 3.4

$d_0$  – diameter of hole

	$k_1 \perp$ Direction perpendicular to force
Inner	$\min (1,4 p_2 / d_0 - 1,7 ; 2,5)$
Edge	$\min (2,8 e_2 / d_0 - 1,7 ; 2,5)$

	$\alpha_d \parallel$ Direction parallel to force
Inner	$p_1 / 3d_0 - 0,25$
End	$e_1 / 3d_0$

Index 1 and 2 in symbols  $e_1$   $e_2$   $p_1$   $p_2$  - there are no horizontal H and vertical V directions, but always parallel (1)  $\parallel$  and perpendicular (2)  $\perp$  to direction of force:

→ Des #2 examp 1 / 73

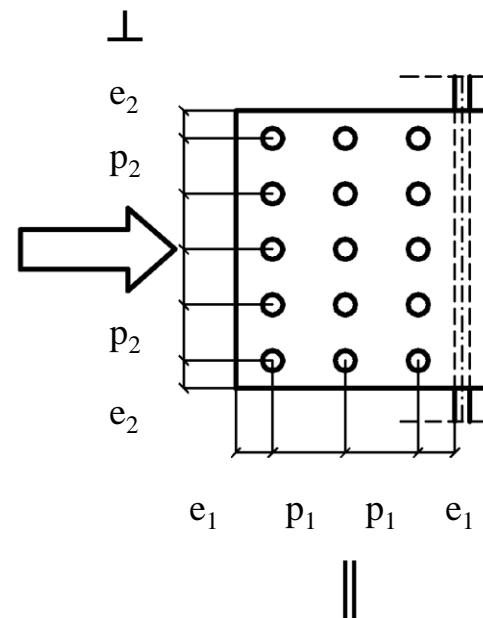
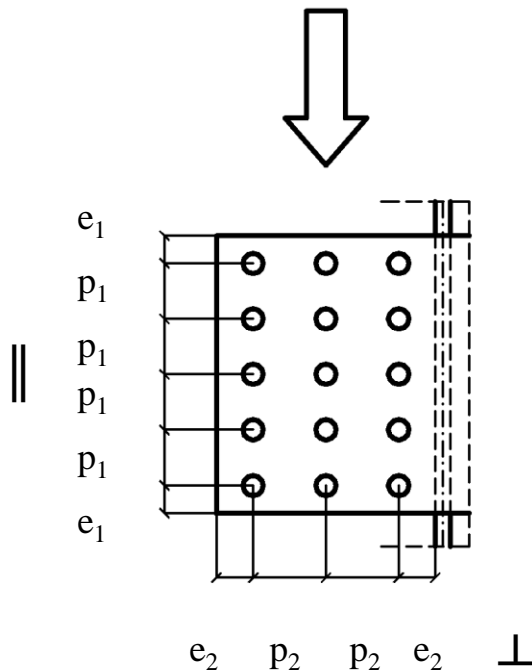
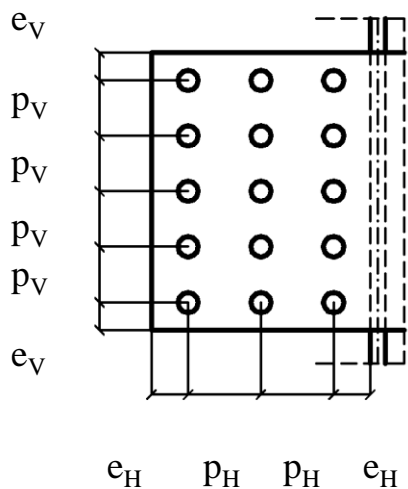
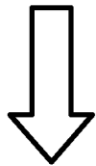


Photo: Author

	$k_1 \perp$	Notice
<b>Inner</b>	$\min(1,4 p_2 / d_0 - 1,7 ; 2,5)$	Neighboring bolts on <b>both sides</b> $\perp$ to force
<b>Edge</b>	$\min(2,8 e_2 / d_0 - 1,7 ; 2,5)$	Neighboring bolts on <b>one side only</b>



$k_1 \perp \rightarrow$  Des #2 examp 1 / 74

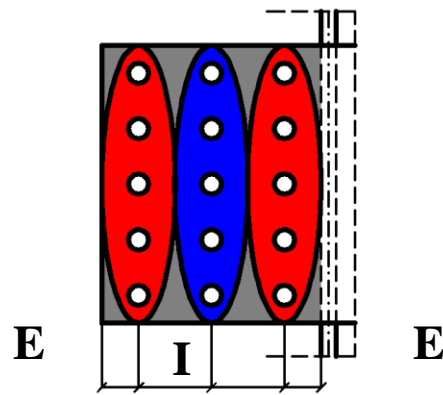
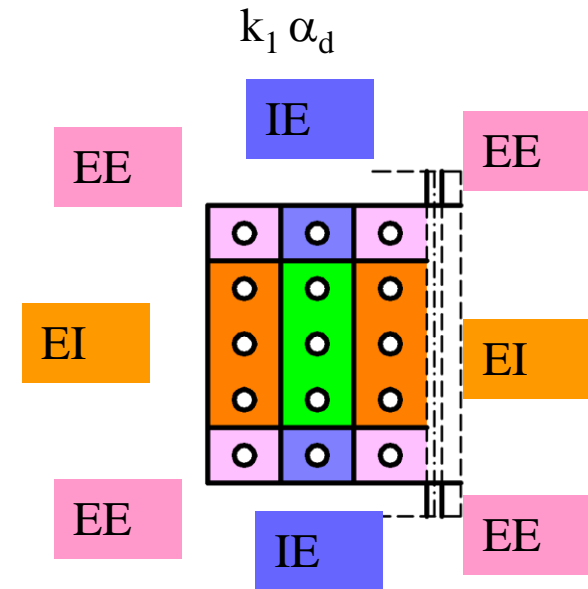
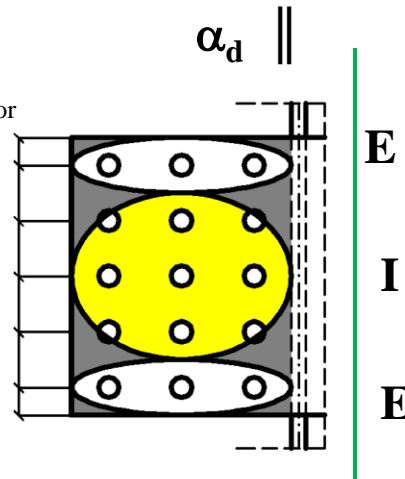


Photo: Author

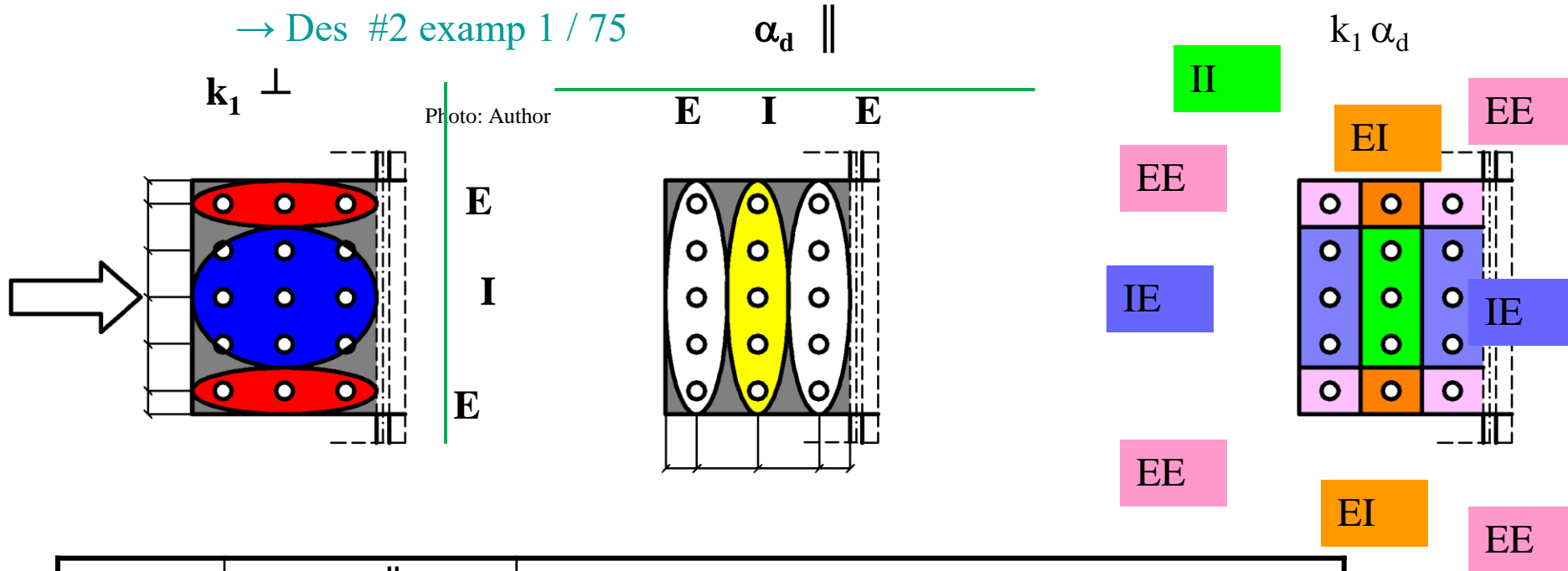


	$\alpha_d \parallel$	Notice
<b>Inner</b>	$p_1 / 3d_0 - 0,25$	Neighboring bolts on <b>both sides</b> $\parallel$ to force
<b>End</b>	$e_1 / 3d_0$	Neighboring bolts on <b>one side only</b>

**II**

	$k_1 \perp$	Notice
<b>Inner</b>	$\min(1,4 p_2 / d_0 - 1,7 ; 2,5)$	Neighboring bolts on <b>both sides</b> $\perp$ to force
<b>Edge</b>	$\min(2,8 e_2 / d_0 - 1,7 ; 2,5)$	Neighboring bolts on <b>one side only</b>

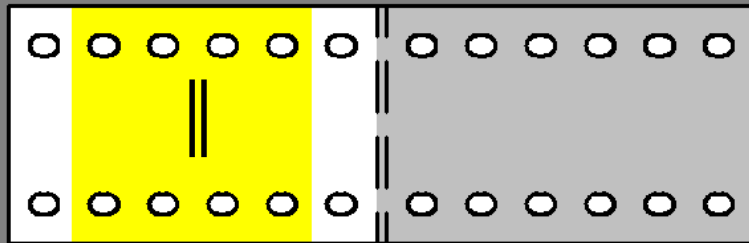
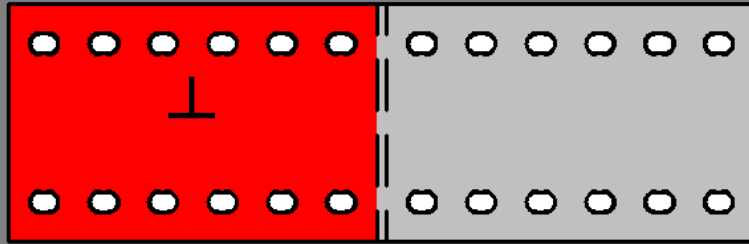
→ Des #2 examp 1 / 75



	$\alpha_d \parallel$	Notice
<b>Inner</b>	$p_1 / 3d_0 - 0,25$	Neighboring bolts on <b>both sides</b> $\parallel$ to force
<b>End</b>	$e_1 / 3d_0$	Neighboring bolts on <b>one side only</b>

Edge

No inner



End

Inner

End

Photo: Author

	$k_1 \perp$ Direction perpendicular to force
Inner	$\min (1,4 p_2 / d_0 - 1,7 ; 2,5)$
Edge	$\min (2,8 e_2 / d_0 - 1,7 ; 2,5)$

$d_0 = (\text{slotted hole: } l) = 36 \text{ mm}$

	$\alpha_d \parallel$ Direction parallel to force
Inner	$p_1 / 3d_0 - 0,25$
End	$e_1 / 3d_0$

$d_0 = 26 \text{ mm}$

	$k_1 \perp$
Inner	
Edge	2,189

$$f_{ub} / f_u = 800 / 360 = 2,222$$

	$\alpha_d \parallel$	$\alpha_b = \min(\alpha_d; f_{ub} / f_u; 1,0) \parallel$
Inner	0,765	0,765
End	0,641	0,641

   $\beta_b = 0,8$

**End** **Edge**

$$F_{b,Rd} = \beta_b k_1 \alpha_b f_u d t_{\min} / \gamma_{M2} = 0,8 \cdot 2,189 \cdot 0,641 \cdot 800 \text{ MPa} \cdot 24 \text{ mm} \cdot 26 \text{ mm} / 1,25 = 448,289 \text{ kN}$$

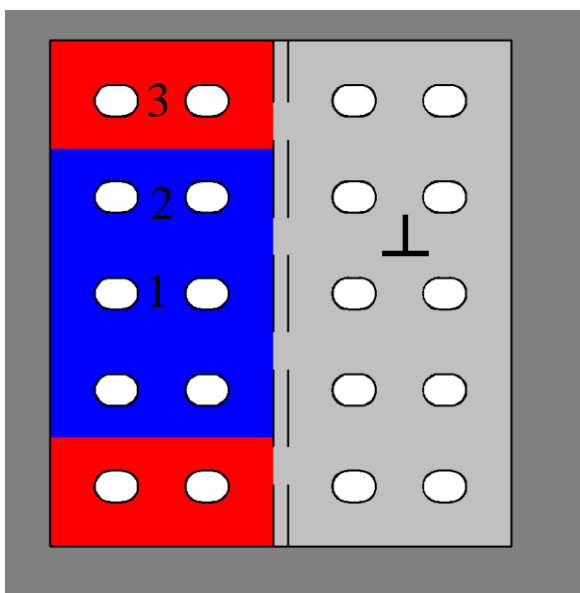
$$86,477 / 448,289 = 0,193 < 1,0 \quad \text{OK}$$

**Inner** **Edge**

$$F_{b,Rd} = \beta_b k_1 \alpha_b f_u d t_{\min} / \gamma_{M2} = 0,8 \cdot 2,189 \cdot 0,765 \cdot 800 \text{ MPa} \cdot 24 \text{ mm} \cdot 26 \text{ mm} / 1,25 = 535,019 \text{ kN}$$

$$86,477 / 535,019 = 0,162 < 1,0 \quad \text{OK}$$

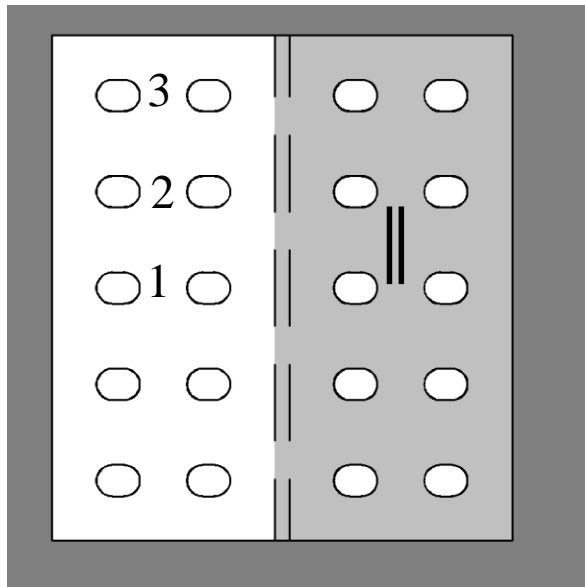
Edge



Inner

Edge

Photo: Author



End

No inner

	$k_1 \perp$ Direction perpendicular to force
Inner	$\min (1,4 p_2 / d_0 - 1,7 ; 2,5)$
Edge	$\min (2,8 e_2 / d_0 - 1,7 ; 2,5)$

$d_0 = 26 \text{ mm}$



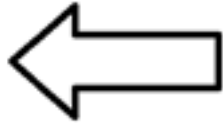
	$\alpha_d \parallel$ Direction parallel to force
Inner	$p_1 / 3d_0 - 0,25$
End	$e_1 / 3d_0$

$d_0 = (\text{slotted hole: } l) = 36 \text{ mm}$

	$k_1 \perp$
Inner	2,500
Edge	2,500

$$f_{ub} / f_u = 800 / 360 = 2,222$$

	$\alpha_d \parallel$	$\alpha_b = \min(\alpha_d; f_{ub} / f_u; 1,0) \parallel$
Inner		
End	0,463	0,463



Resistances for horizontal forces:

   $\beta_b = 0,8$

**End** **Edge** 3

$$F_{b,Rd} = \beta_b k_1 \alpha_b f_u d t_{\min} / \gamma_{M2} = 0,8 \cdot 2,500 \cdot 0,463 \cdot 800 \text{ MPa} \cdot 24 \text{ mm} \cdot 13,5 \text{ mm} / 1,25 = 192,015 \text{ kN}$$

**End** **Inner** 2 1

$$F_{b,Rd} = \beta_b k_1 \alpha_b f_u d t_{\min} / \gamma_{M2} = 0,8 \cdot 2,500 \cdot 0,463 \cdot 800 \text{ MPa} \cdot 24 \text{ mm} \cdot 13,5 \text{ mm} / 1,25 = 192,015 \text{ kN}$$

Edge

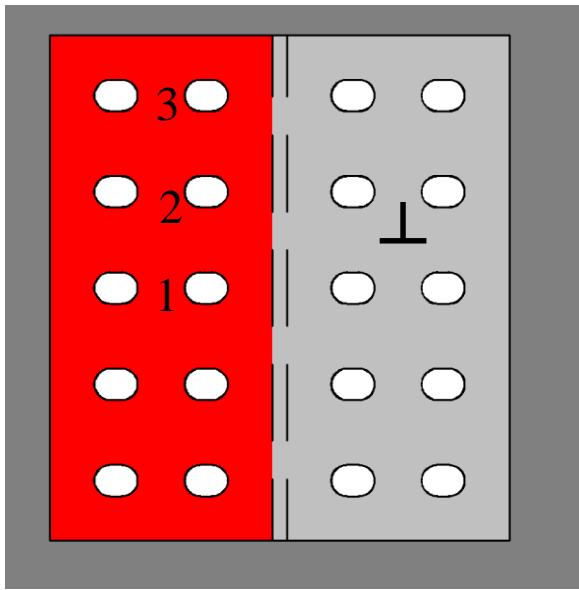
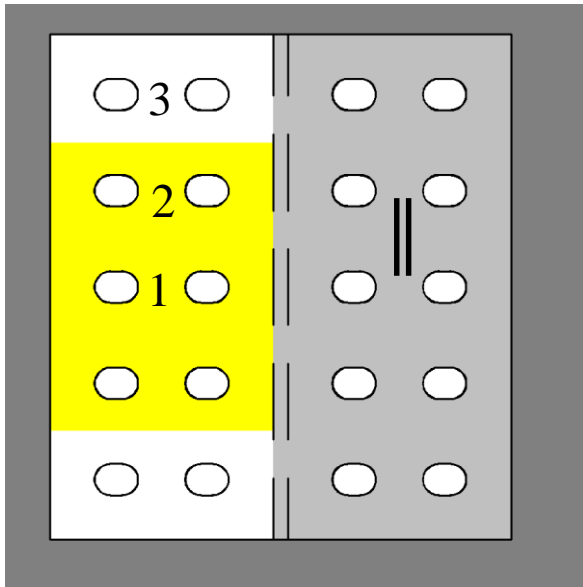


Photo: Author

End

Inner

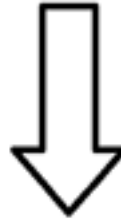
End



No inner

	$k_1 \perp$ Direction perpendicular to force
Inner	$\min (1,4 p_2 / d_0 - 1,7 ; 2,5)$
Edge	$\min (2,8 e_2 / d_0 - 1,7 ; 2,5)$

$$d_0 = (\text{slotted hole: } l) = 36 \text{ mm}$$



	$\alpha_d \parallel$ Direction parallel to force
Inner	$p_1 / 3d_0 - 0,25$
End	$e_1 / 3d_0$

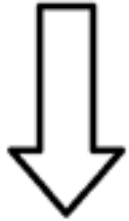
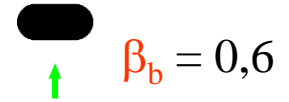
$$d_0 = 26 \text{ mm}$$

	$k_1 \perp$
Inner	
Edge	2,189

$$f_{ub} / f_u = 800 / 360 = 2,222$$

Photo: Author

	$\alpha_d \parallel$	$\alpha_b = \min(\alpha_d; f_{ub} / f_u; 1,0) \parallel$
Inner	0,776	0,776
End	0,641	0,641



Resistances for vertical forces:

**End** **Edge** 3

$$F_{b,Rd} = \beta_b k_1 \alpha_b f_u d t_{min} / \gamma_{M2} = 0,6 \cdot 2,189 \cdot 0,641 \cdot 800 \text{ MPa} \cdot 24 \text{ mm} \cdot 13,5 \text{ mm} / 1,25 = 174,574 \text{ kN}$$

**Inner** **Edge** 2 1

$$F_{b,Rd} = \beta_b k_1 \alpha_b f_u d t_{min} / \gamma_{M2} = 0,6 \cdot 2,189 \cdot 0,776 \cdot 800 \text{ MPa} \cdot 24 \text{ mm} \cdot 13,5 \text{ mm} / 1,25 = 211,341 \text{ kN}$$

Web, checking resistance:

Bolt	Force H	Force V	Resistance H	Resistance V	E / R H	E / R V
1	0,000	47,126	192,015	174,574	0,000	0,270
2	65,975	47,126	192,015	174,574	0,343	0,270
3	131,835	47,126	192,015	211,341	0,687	0,223

Corner bolt: max values of loads (from bending moment), probably min resistance (because of small e)

Everything's all right.

In case of problems, it is recommended to add another column of bolts. Then, calculation must be made once again since slide #19.

Slip-resistant: preloaded bolts; initial non-zero value of axial tensile force in shank (as a effect of tight twisting of hex nut) → non-zero value of compressive force between plates → friction between plates. Destruction: value of load bigger than friction.

$$F_{s,Rd} = k_s n \mu F_{p,C} / \gamma_{M3} \quad \text{EN 1993-1-8 p.3.9.1}$$

$$\gamma_{M3} = 1,25$$

$$F_{p,C} \rightarrow \#t / 66$$

$$k_s \text{ EN 1993-1-8 tab 3.6 } (\rightarrow \#t / 66)$$

$$\mu \text{ EN 1993-1-8 tab 3.7 } (\rightarrow \#t / 67)$$

(Class of surface  $\neq$  category of joint)

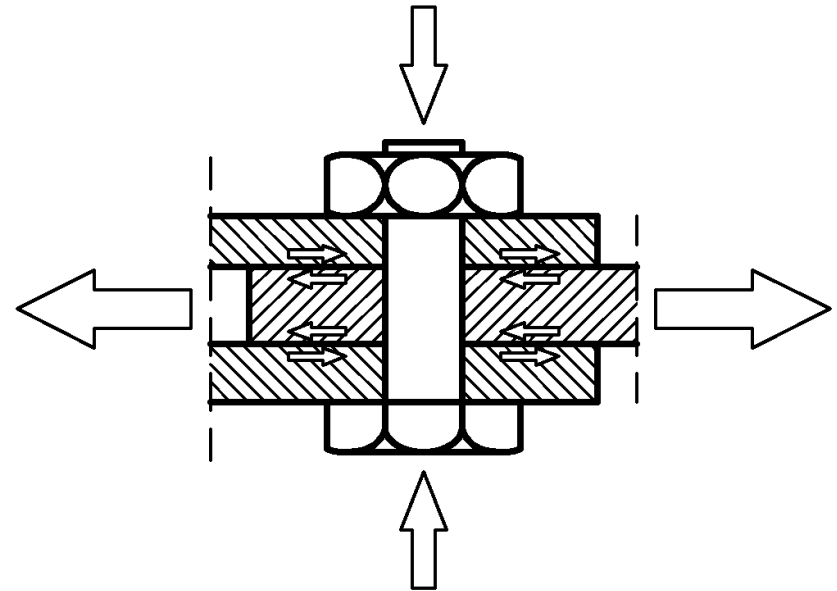







Photo: Author

$$F_{p,C} = 0,7 f_{ub} A_s / \gamma_{M7} = 0,636 f_{ub} A_s = 88\% \text{ tensile force resistance} = 0,720 f_{ub} A_s$$

$$\gamma_{M7} = 1,1$$

EN 1993-1-8 (3.7)

Type of holes		Force	$k_s$
Round	Fit		1,0
	Normal		1,0
	Oversized		0,85
Slotted	Short		0,76
			0,85
	Long		0,63
			0,70

EN 1993-1-8 tab. 3.6

Photo: Author

EN 1993-1-8 tab. 3.7

EN 1090-2 tab 18

Class of friction surfaces	Friction coefficient $\mu$	Surface treatment
A	0,5	Surface blasted with shot or grit with loose rust removed, not pitted;
B	0,4	Surfaces blasted with shot or grit: <ul style="list-style-type: none"><li>◆ spray-metallized with a aluminum or zinc based product;</li><li>◆ with alkali-zinc silicate paint with a thickness of 50 <math>\mu\text{m}</math> to 80 <math>\mu\text{m}</math>;</li></ul>
C	0,3	Surfaces cleaned by wire-brushing or flame cleaning, with loose rust removed;
D	0,2	Surfaces as rolled;

## Flange

$$F_{s,Rd} = k_s n \mu F_{p,C} / \gamma_{M3}$$

$$\gamma_{M3} = 1,25$$

$k_s$  for long slotted holes = 0,63

$\mu$  taken into consideration 0,5 (class of surface A)

$$F_{p,C} = 0,7 f_{ub} A_s = 197,680 \text{ kN}$$

$$F_{s,Rd} = k_s n \mu F_{p,C} / \gamma_{M3} = 49,815 \text{ kN}$$

Bolted category B:

load calculated for **characteristic value**

$$F_{b,k} = 57,985 \text{ kN}$$

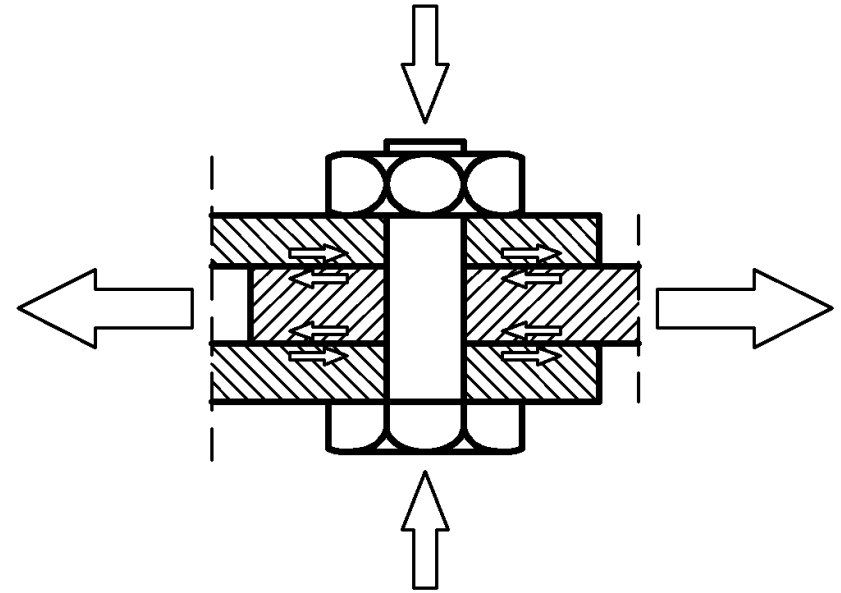
$$E/R = 57,985 / 49,815 = 1,164 > 1,0 \quad \text{WRONG}$$

More bolts must be applied:  $12 \cdot 1,164 = 14$  bolts

At now, force in bolt =  $(57,985 \cdot 12) / 14 = 49,701 \text{ kN}$

$$E/R = 49,701 / 49,815 = 0,998 < 1,0 \quad \text{OK}$$

Photo: Author



Full information about bolts in flange; verification of shear resistance

Formula for resistance of bolt under shear force is:

$$F_{v,Rd, total} = n \beta_{12-14} \beta_{Lf} \beta_p \alpha_V f_{ub} A_{(s)} / \gamma_{M2}$$

**Part taken into consideration** ( $\rightarrow$  #t / 50)

$\beta_{12-14}$  – important for M12, M14 only

$\beta_p$  – important for various cross-sections of two I-beams on left and right side of joints

$\beta_{Lf}$  – impact of length of joint

At now, when total number of bolts in flange / flange plate is known (effect of checking resistance for shear force and slip-resistant), impact of length for shear force resistance must be analysed.

Condition 1:  $\sqrt{[(\sigma_{\perp})^2 + 3(\tau_{\parallel}^2 + \tau_{\perp}^2)]} \leq b_{LW} f_u / (\beta_w \gamma_{M2})$

Condition 2:  $\sigma_{\perp} \leq 0,9 b_{LW} f_u / \gamma_{M2}$

→ #17 / 69

Values of  $\beta_{LW}$  for different types and lengths of welds:

Length of weld:	0 - ∞		
Between flange and web in welded I-beam	1,0		
Length of weld:	L < 1,700 m	1,700 m < L < 8,500 m	L > 8,500 m
Between transverse stiffeners and plates in welded I-beam	1,0	1,1 - L / 17	0,6
Length of weld:	L < 150 a	150 a < L < 900 a	L > 900 a
All other cases	1,0	1,2 - 0,2 L / (150 a)	0,0

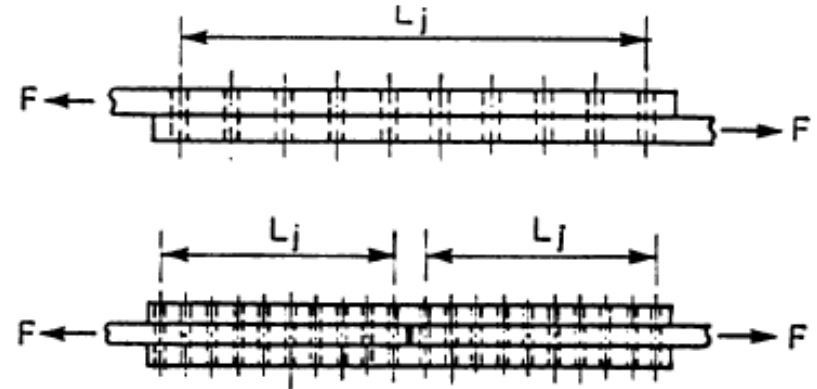
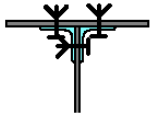
EN 1993-1-8 (4.9), (4.10)

In full analogy to welds: long joints for bolted joint:

Photo: EN 1993-1-8 fig. 3.7

EN 1993-1-8 3.8

Photo: Author



$b_{Lf}$  :

	$L_j \leq 15 d$	$15 d \leq L_j \leq 65 d$	$L_j \geq 65 d$
Uniform distribution of force transfer over the length of the joint (flange-web)	1,00		
All other cases	1,00	$1 - (L_j - 15 d) / (200 d)$	0,75

7 pairs of bolts:

Photo: EN 1993-1-8 fig. 3.7

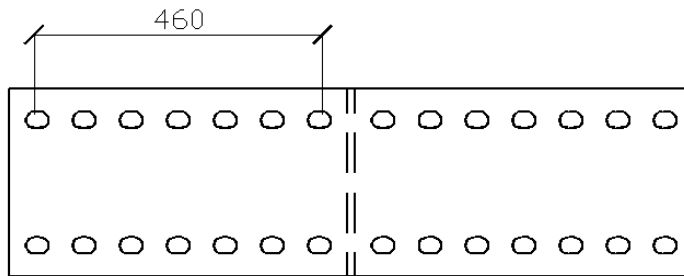
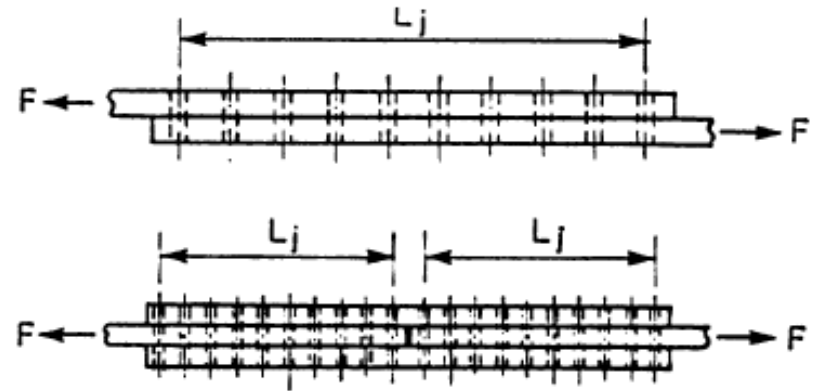


Photo: Author



$$15 d = 360 \text{ mm} < L_j = 460 \text{ mm} < 65 d = 1\,560 \text{ mm}$$

$$b_{Lf} = 1 - (L_j - 15 d) / (200 d) = 0,979$$

Resistance for shear force is not 173,568 kN ( $\rightarrow \#t / 50$ ),

but  $0,979 \cdot 173,568 \text{ kN} = 169,923 \text{ kN}$

$86,477 / 169,923 = 0,509 < 1,0$  **OK**

Web

$$F_{s,Rd} = k_s n \mu F_{p,C} / \gamma_{M3}$$

$$\gamma_{M3} = 1,25$$

$k_s$  min for long slotted holes = 0,63

$\mu$  taken into consideration 0,5 (class of surface A)

$$F_{p,C} = 0,7 f_{ub} A_s = 197,680 \text{ kN}$$

$$F_{s,Rd} = k_s n \mu F_{p,C} / \gamma_{M3} = 99,631 \text{ kN}$$

Bolted category B:

load calculated for **characteristic value**

max product = 95,763 kN

$$E/ R = 95,763 / 99,631 = 0,961 < 1,0 \quad \text{OK}$$

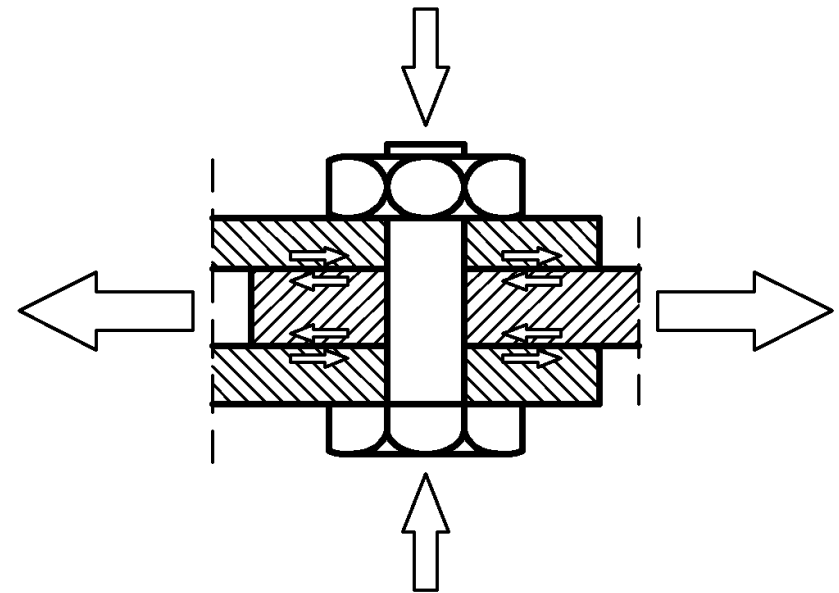


Photo: Author

Punching resistance: as a effect of axial force in bolt (from preloading or load), cap or nut is punched through the plate.

$$B_{p,Rd} = 0,6 \pi d_m t_p f_u / \gamma_{M2}$$

$$d_m = (D + s) / 2$$

EN 1993-1-8 tab 3.4

$$\gamma_{M2} = 1,25$$

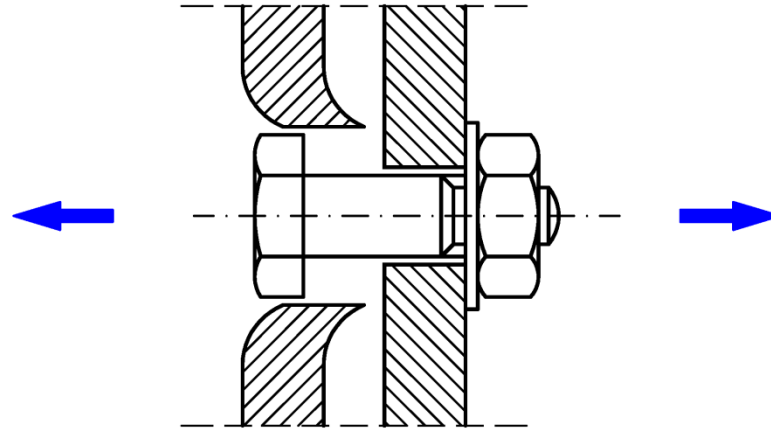


Photo: Author

Load: preloaded force, **the same for web and flange**:  $F_{p,C} = 0,7 f_{ub} A_s = 197,680 \text{ kN}$

The lowest resistance: for web plate,  $t_p = 12 \text{ mm}$

$$B_{p,Rd} = 238,716 \text{ kN}$$

$$E / R = 197,690 / 238,716 = 0,828 < 1,0 \quad \text{OK}$$

## Block tearing (total destruction of plate)



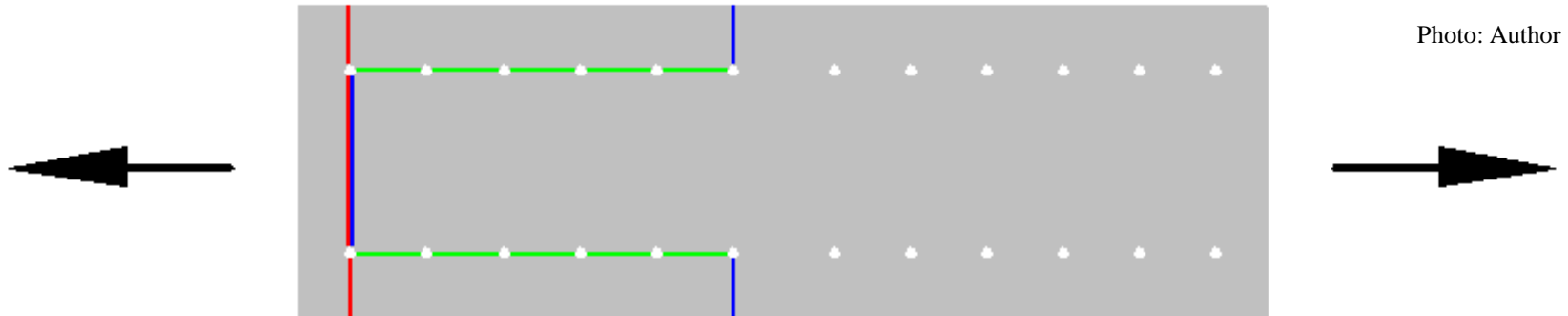
Photo: quora.com

## Netto area (other type of total destruction of plate)



Photo: quora.com

Member	Netto area	Block tearing
Flange plate	1037,724 kN	
Web plate	117,030 kNm and 162,200 kN	Many various loads, not checking
I-beam	727,800 kNm and 162,200 kN	



Flange plate, axial force only. According to #Des 2 Ex1 / 83 we should calculate block tearing (**tension part** and **shear part**), but the smallest area is for **red** cross-section for netto area effect. Netto resistance for tensile axial force:

$$N_{u,Rd} = \min [ 0,9 A_{net} f_u / \gamma_{M2} ; A f_y / \gamma_{M0} ]$$

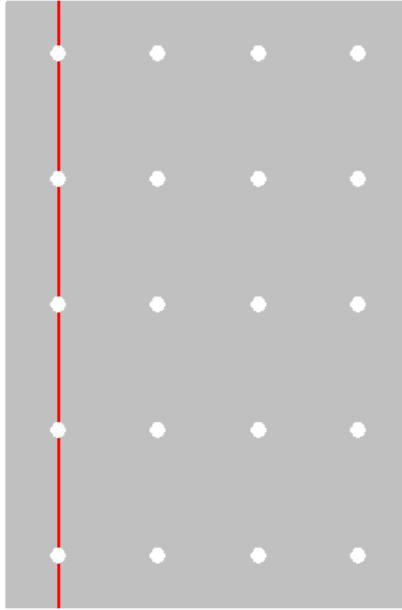


Photo: Author

Web plate, bending moment, shear force and, optionally, axial force.

$$\sigma(N_{fp}) = N_{fp} / A_{netto}$$

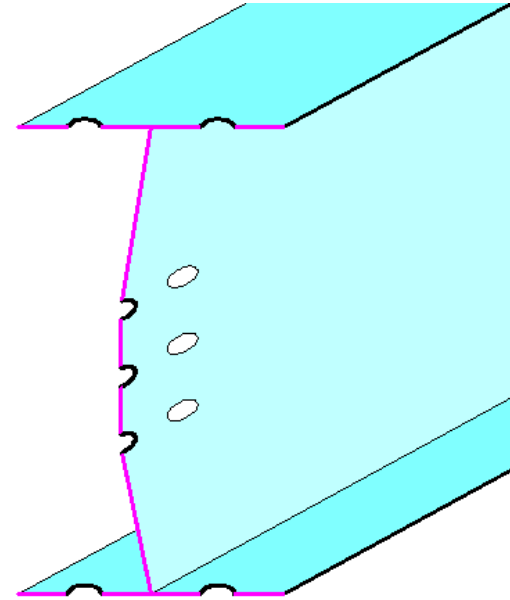
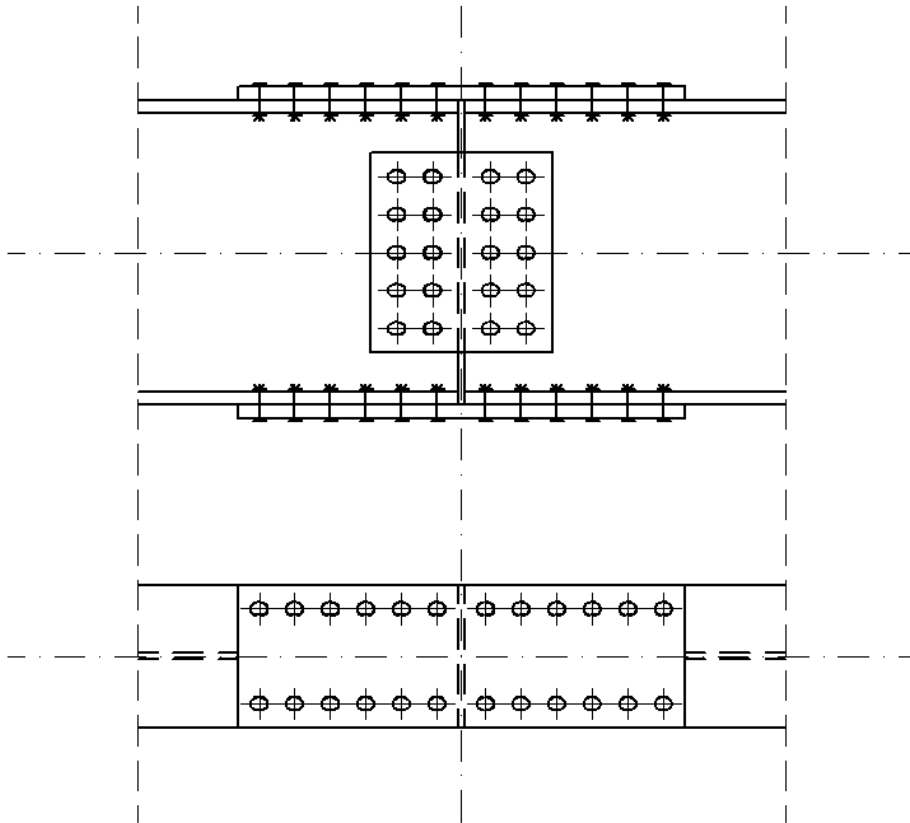
$$\sigma(M_{fp}) = M_{fp} / W_{netto}$$

$$\tau(V_{fp}) = V_{fp} / A_{total}$$

$$\sqrt{\{ [\sigma(N_{fp}) + \sigma(M_{fp})]^2 + 3[\tau(V_{fp})]^2 \}} \leq f_y$$

Web, flange - uniform cross-section, not two separate part. We should analysed destruction of whole netto cross-section.

Photo: Author



$$\sigma(M_{fp}) = M_{Ed} / W_{netto}$$

$$\tau(V_{fp}) = V_{Ed} / (h_w t_w)$$

$$\sqrt{\{ [\sigma(M_{fp})]^2 + 3[t(V_{fp})]^2 \}} \leq f_y$$

Flange plate:  $N_{u,Rd} = \min [ 0,9 A_{net} f_u / \gamma_{M2} ; A f_y / \gamma_{M0} ]$   
 $A_{net} = 74,40 \text{ cm}^2 \quad A = 90 \text{ cm}^2 \quad f_y = 235 \text{ MPa} \quad f_u = 360 \text{ MPa}$   
 $N_{u,Rd} = \min (2 \ 142,720 \text{ kN} ; 2 \ 115,000 \text{ kN}) = 2 \ 115,000 \text{ kN}$   
 $E / R = 1 \ 037,721 / 2 \ 115,000 = 0,491 < 1 \text{ OK}$

Element	Force [kN]	Bending moment [kNm]	$A_v$ [cm <sup>2</sup> ]	W [cm <sup>3</sup> ]	$\sigma$ [MPa]	$\tau$ [MPa]	$\sigma_{eq}$ [MPa]	$\sigma_{eq} / f_y$
Web plate	162,200	117,030	100,80	515,429	227,577	16,091	229,454	<b>0,976</b>
HEA 650	162,200	727,800	86,40	4 594,696	158,400	18,773	161,703	<b>0,688</b>

$A_v$  – total  
W – netto

Thank you for attention

© 2024 Tomasz Michałowski, PhD

[tmichal@pk.edu.pl](mailto:tmichal@pk.edu.pl)