

u, w - skalary

$\vec{V}$ ,  $\vec{Z}$  - wektory ( $V_x; V_y; V_z$ ), ( $Z_x; Z_y; Z_z$ )

## OPERATORY:

**nabla *vel* hamiltonian (wektor):**

$$\vec{\nabla} = (\partial/\partial x; \partial/\partial y; \partial/\partial z)$$

$$\vec{\nabla} u = \text{grad } u = (\partial u/\partial x; \partial u/\partial y; \partial u/\partial z) = \vec{Z} \text{ (gradient)}$$

$$\vec{\nabla} \circ \vec{V} = \text{div } \vec{V} = \partial V_x/\partial x + \partial V_y/\partial y + \partial V_z/\partial z = w \text{ (dywergencja)}$$

$$\vec{\nabla} \times \vec{V} = \text{rot } \vec{V} = (\partial V_z/\partial y - \partial V_y/\partial z; \partial V_x/\partial z - \partial V_z/\partial x; \partial V_y/\partial x - \partial V_x/\partial y) = \vec{Z} \text{ (rotacja)}$$

**laplasjan (skalar):**

$$\Delta = \vec{\nabla} \circ \vec{\nabla} = \partial^2/\partial x^2 + \partial^2/\partial y^2 + \partial^2/\partial z^2$$

$$\Delta u = \partial^2 u/\partial x^2 + \partial^2 u/\partial y^2 + \partial^2 u/\partial z^2 = w$$

$$\Delta \vec{V} = (\partial^2 V_x/\partial x^2 + \partial^2 V_x/\partial y^2 + \partial^2 V_x/\partial z^2 ; \\ \partial^2 V_y/\partial x^2 + \partial^2 V_y/\partial y^2 + \partial^2 V_y/\partial z^2 ; \\ \partial^2 V_z/\partial x^2 + \partial^2 V_z/\partial y^2 + \partial^2 V_z/\partial z^2) = \vec{Z}$$